

This webinar is being recorded  
and will be published online

January 29th 2024

15:00 – 16:30 CET,

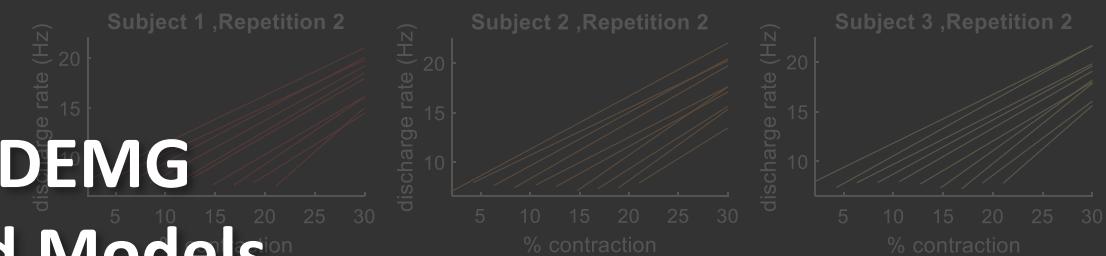
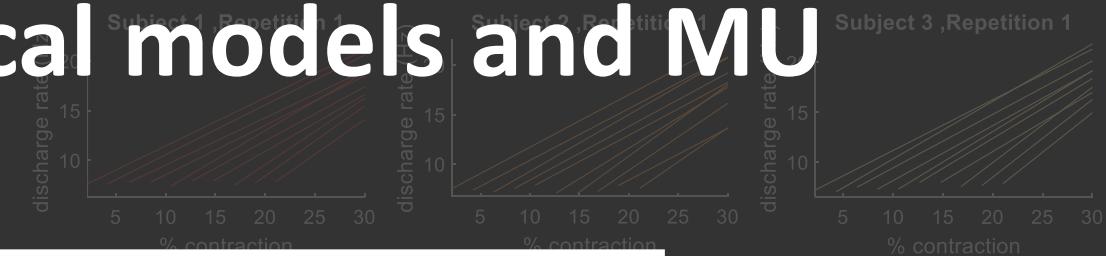
9:00 – 10:30 EST

# WEBINAR:

## Validation of results: statistical models and MU identification accuracy

### Gentle introduction to:

- Accuracy of MU identification from HDEMG
- Regression analysis with Linear Mixed Models
- Bayesian Linear Regression Models



Lecturers: Aleš Holobar, Nina Murks  
University of Maribor, Slovenia



## Hybrid neuroscience based on cerebral and muscular information for motor rehabilitation and neuromuscular disorders



HybridNeuro focuses on development of Hybrid Neural-machine Interfaces, which record cerebral and muscular signals, and aims to improve the objectivity, precision and personalisation of monitoring and rehabilitation of neuromuscular disorders, such as stroke.



Funded by  
the European Union



UK Research  
and Innovation



University of Maribor



UNIVERSITAT POLITÈCNICA  
DE CATALUNYA  
BARCELONATECH



CHALMERS  
UNIVERSITY OF TECHNOLOGY

Imperial College  
London

This project has received funding from the European Union's Horizon Europe Research and Innovation Programme under grant agreement no. 101079392 and from the UK Research and Innovation (UKRI) government's Horizon Europe funding guarantee scheme under grant agreement no. 10052152.



## Hybrid neuroscience based on cerebral and muscular information for motor rehabilitation and neuromuscular disorders

### Our mission:

- 1 Exploratory research project for development of Hybrid Neural-machine Interfaces
- 2 Summer schools
- 4 Workshops
- 8 Webinars
- 1 Biomedical Signals Data Repository
- 1 Massive open online course (MOOC) on Hybrid Neuroscience
- 1 International HybridNeuro Hub
- 12 National/international events

Visit us at:

<https://www.hybridneuro.feri.um.si>

<https://twitter.com/hybridneuro>



Funded by  
the European Union



UK Research  
and Innovation



CHALMERS  
UNIVERSITY OF TECHNOLOGY

Imperial College  
London

This project has received funding from the European Union's Horizon Europe Research and Innovation Programme under grant agreement no. 101079392 and from the UK Research and Innovation (UKRI) government's Horizon Europe funding guarantee scheme under grant agreement no. 10052152.

February 6<sup>th</sup> –9<sup>th</sup> 2024

Universitat Politècnica de Catalunya, Barcelona, Spain



HYBRID  
NEURO

# WORKSHOP BCN24

## “A journey into brain activity”

*From EEG and related potentials to connectivity and source modeling*

**Day 1: EEG signal acquisition and preprocessing.**

**Day 2: ERP and MRCP studies and movement intention for device control.**

**Day 3: Source localization and brain connectivity.**

**Day 4: Networking with hospitals, companies, and research centers.**



Hybrid Workshop  
(online and In-person event).  
Contact: Bioart.group@upc.edu



REGISTER NOW



Funded by  
the European Union



UK Research  
and Innovation

GA 10052152



University of Maribor



UNIVERSITAT POLITÈCNICA  
DE CATALUNYA  
BARCELONATECH



CHALMERS  
UNIVERSITY OF TECHNOLOGY

Imperial College  
London

GA 101079392



University of Maribor



Imperial College  
London



REGISTER NOW!



UK Research  
and Innovation

GA No. 10052152



Funded by  
the European Union

GA No. 101079392



**FREE REGISTRATION**  
Travel & accommodation costs  
to be covered by participants



# Summer school on **Hybrid Neural Interfaces**

**July 8<sup>th</sup>-12<sup>th</sup> 2024, Maribor, Slovenia**

- Surface & intramuscular HDEMG
- Identification of neural codes
- EEG & functional brain connectivity
- Corticomuscular coupling
- Movement augmentation
- Hybrid Neural Interfaces in practice
- Keynote lectures
- Practical examples
- Student 2 student explanations
- Present your project
- Ask top experts
- Active consultations

January 29th 2024

15:00 – 16:30 CET,

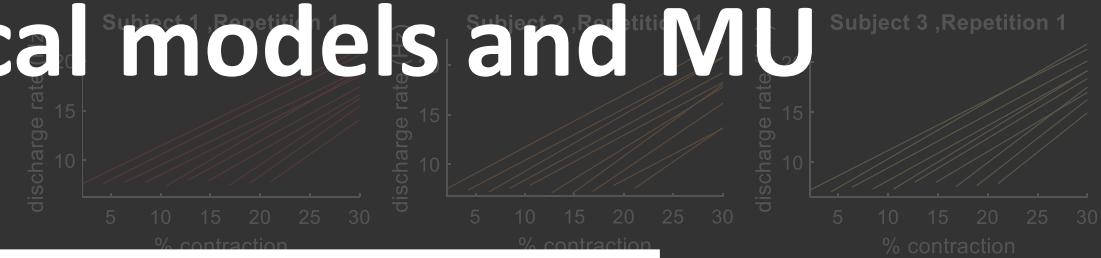
9:00 – 10:30 EST

## WEBINAR:

# Validation of results: statistical models and MU identification accuracy

## Gentle introduction to:

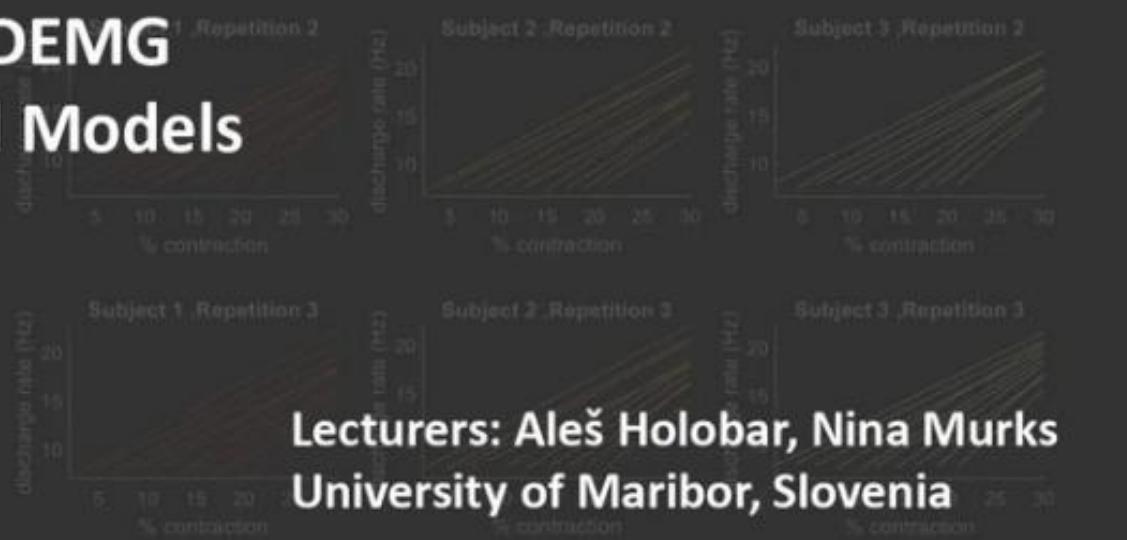
- Accuracy of MU identification from HDEMG
- Regression analysis with Linear Mixed Models
- Bayesian Linear Regression Models



Lecturers: Aleš Holobar, Nina Murks  
University of Maribor, Slovenia

- Accuracy of MU identification from HDEMG
- Regression analysis with Linear Mixed Models
- Bayesian Linear Regression Models

- Use cases & examples in MATLAB & R
- Synthetic & experimental data
- Free registration



Lecturers: Aleš Holobar, Nina Murks  
University of Maribor, Slovenia



Funded by  
the European Union

GA No. 101079392



UK Research  
and Innovation  
GA No. 10052152



University of Maribor



UNIVERSITAT POLITÈCNICA  
DE CATALUNYA  
BARCELONATECH



CHALMERS  
UNIVERSITY OF TECHNOLOGY

Imperial College  
London

Access the webinar content showcased here:

#### MATLAB Code

- Experimental EMG
- Synthetic EMG

#### R Code

- Experimental EMG
- Synthetic EMG

#### Data

- Experimental EMG
- Synthetic EMG
- Large Synthetic EMG

#### Presentation

- Slides

# Files on the HybridNeuro website



- MATLAB:
  - `MATLAB_code_SyntheticEMG.m`: Generation of synthetic data and preliminary statistical analysis
  - `MATLAB_code_ExperimentalEMG.m`: Analysis of experimental data
- DATA:
  - `DATA_SyntheticEMG.csv`: synthetic data (15 subjects, 3 contraction repetitions, 15 MUs per subject, no missed MUs – balanced tests...)
  - `LARGE_DATA_SyntheticEMG.csv`: synthetic data (20 subjects, 3 Contraction repetitions, 20 MUs per subject, no missed MUs – balanced tests...)
  - `DATA_ExperimentalEMG.csv`: experimental data (19 subjects, 3 contraction repetitions, MUs tracked across contraction repetitions)
- RSTUDIO:
  - `R_code_SyntheticEMG.R`: Analysis of synthetic data
  - `R_code_ExperimentalEMG.R`: Analysis of experimental data



Funded by  
the European Union

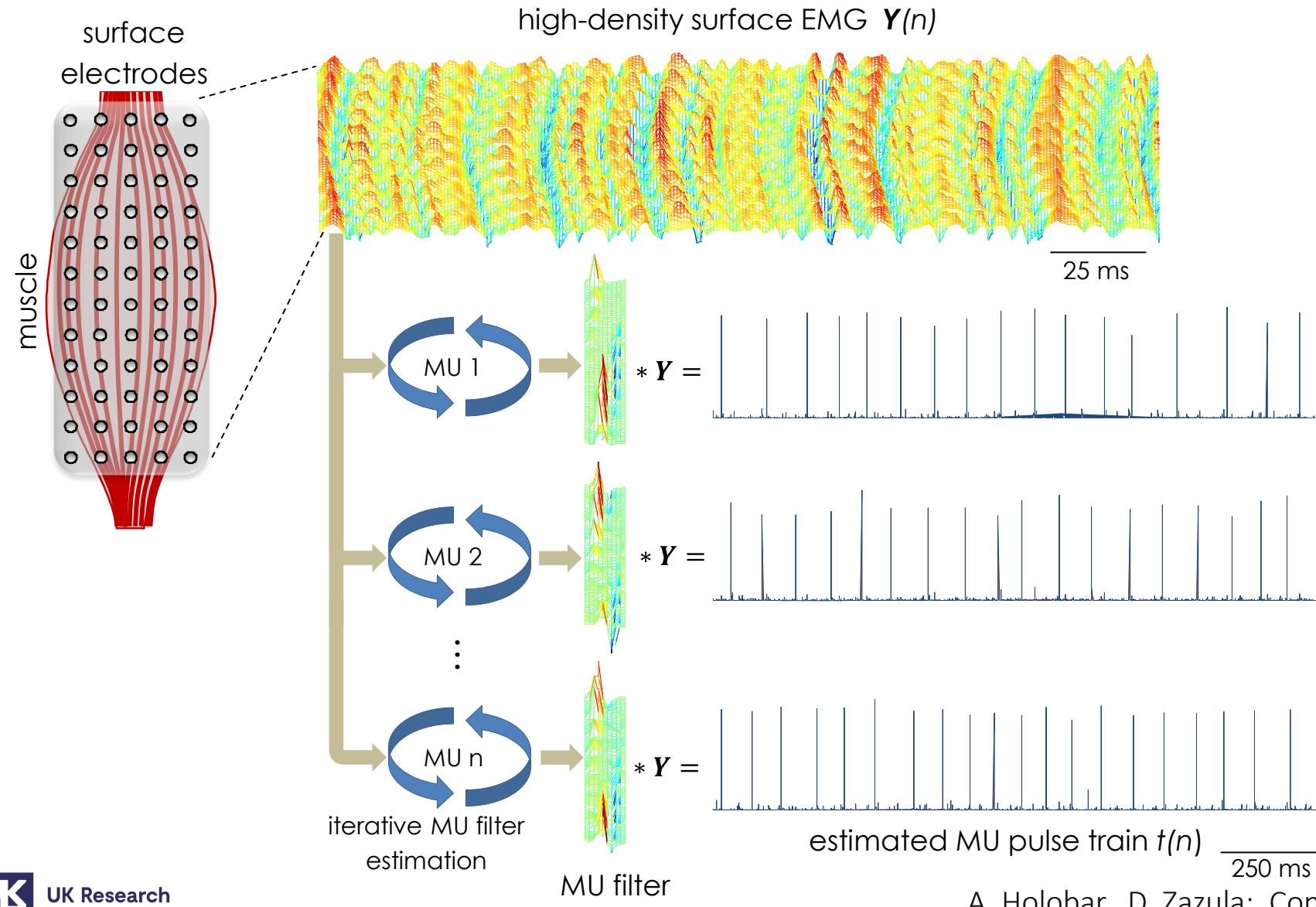


UK Research  
and Innovation

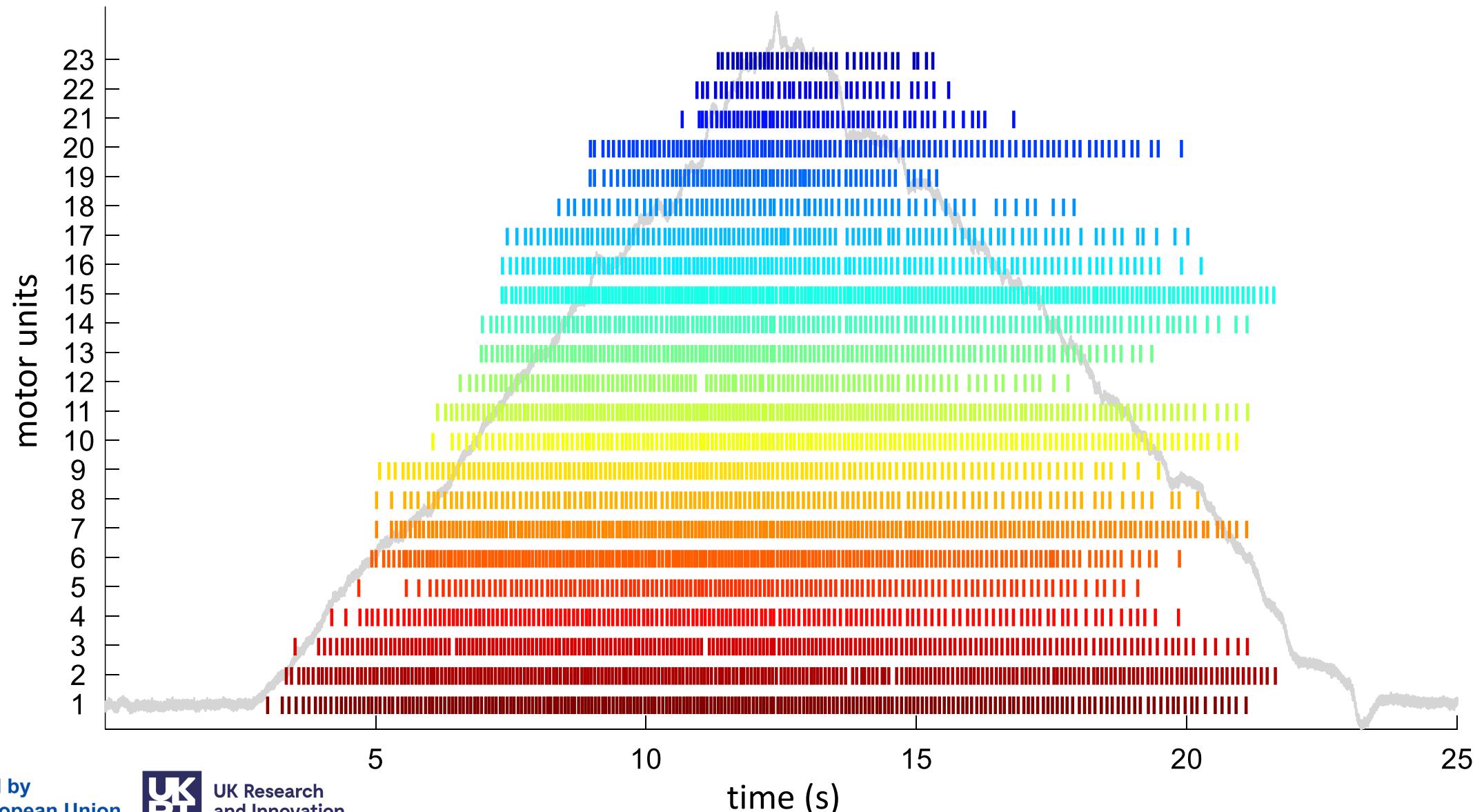
GA No. 101079392

GA No. 10052152

# Identification of MU spike trains: MU filter



# MU discharge patterns



Funded by  
the European Union

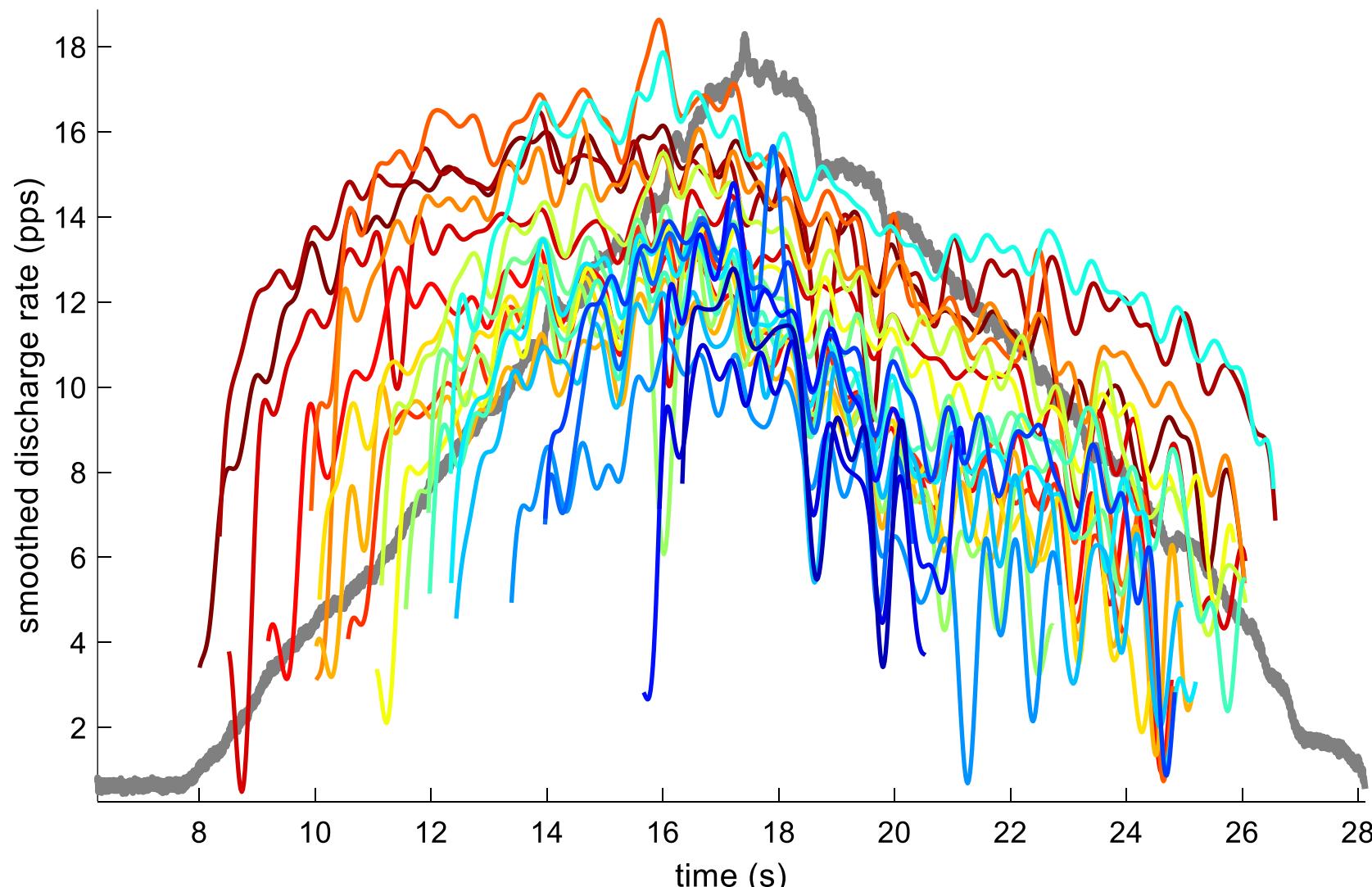
GA No. 101079392



UK Research  
and Innovation

GA No. 10052152

# MU discharge rates



Funded by  
the European Union



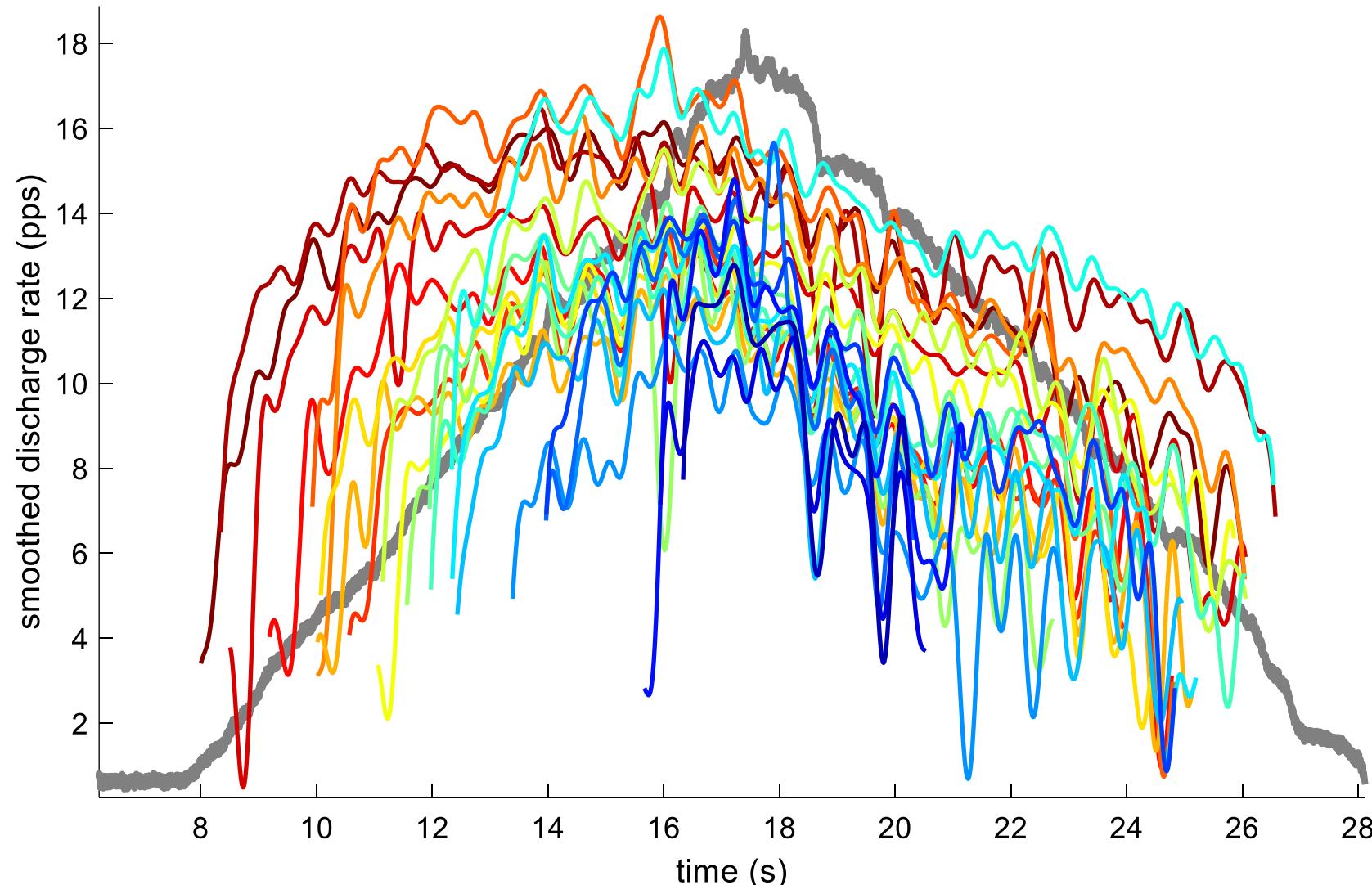
UK Research  
and Innovation

GA No. 101079392

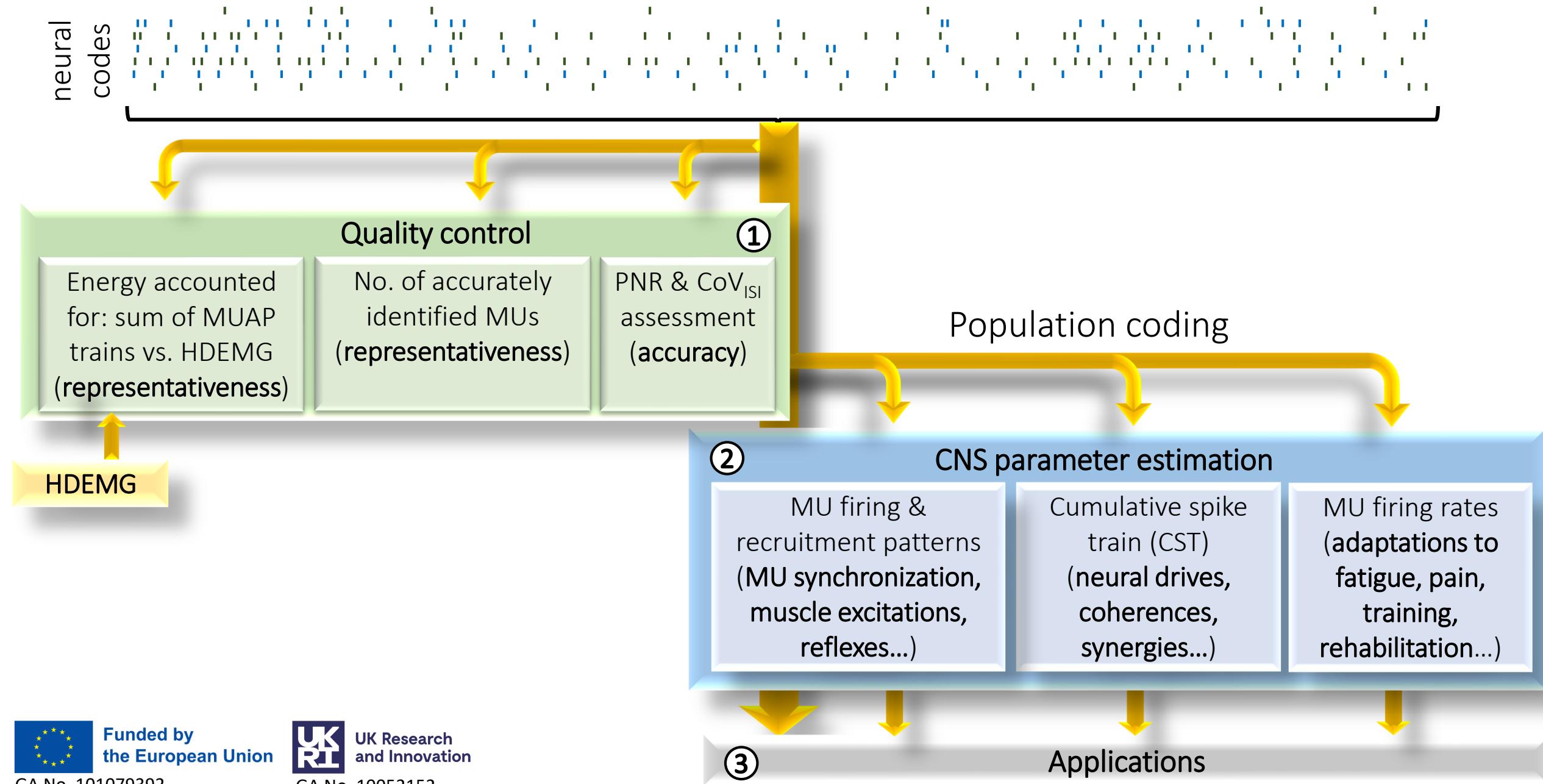
GA No. 10052152

In Wilkinson notation:

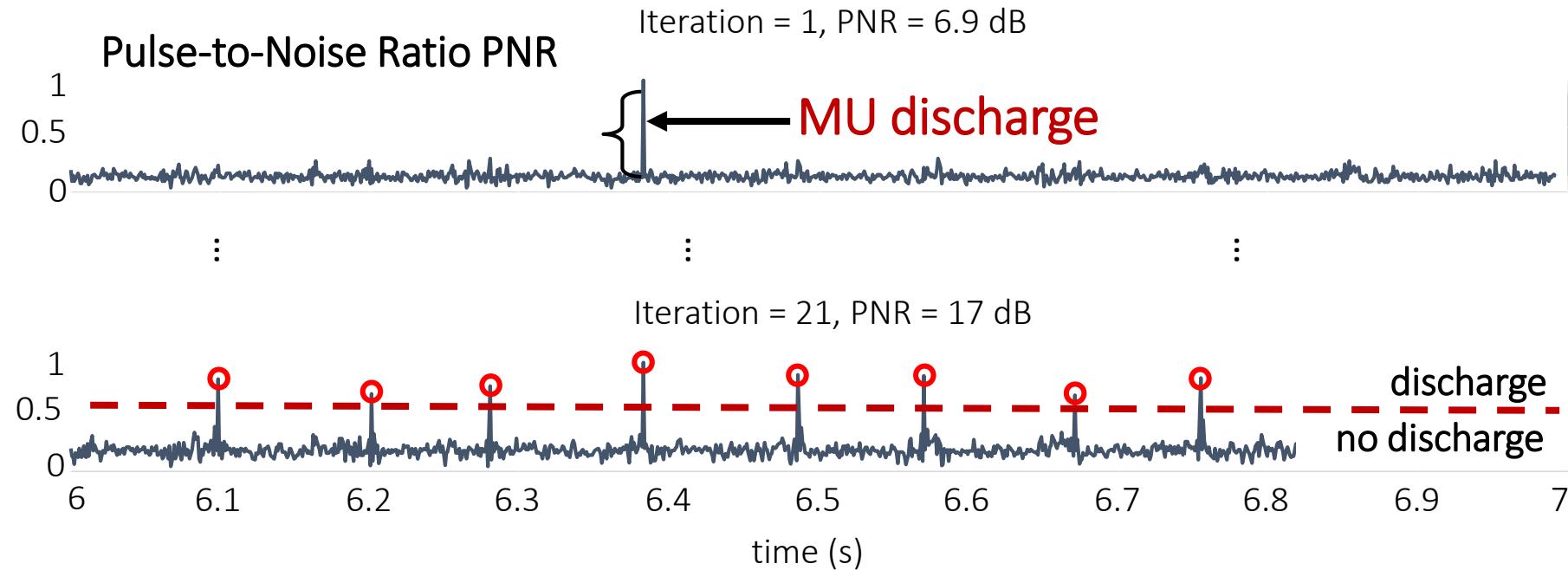
$\text{MaxDR} \sim 1 + \text{RecThr} + \text{RecDR} + (-1 + \text{RecThr} | \text{SubID}) + (-1 + \text{RecThr} | \text{ContRep}) + (-1 + \text{RecThr} | \text{SubID: MUid})$



# Information extraction pipeline



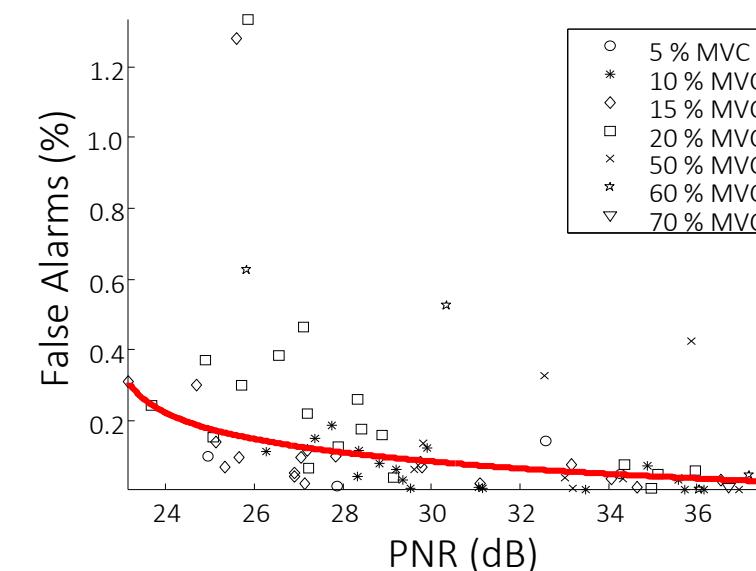
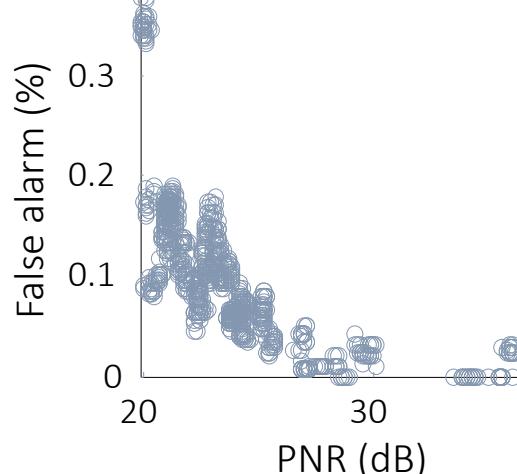
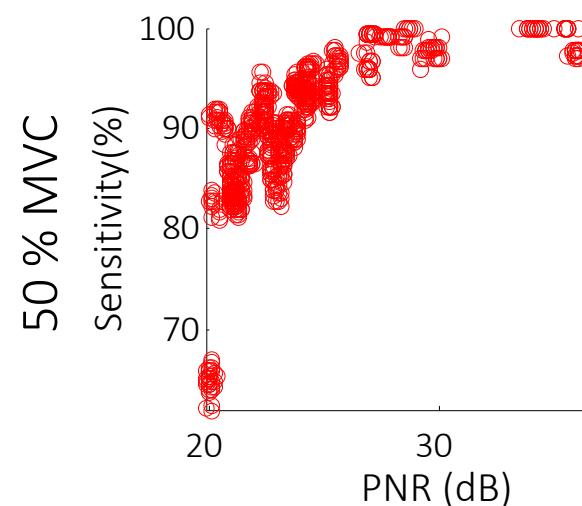
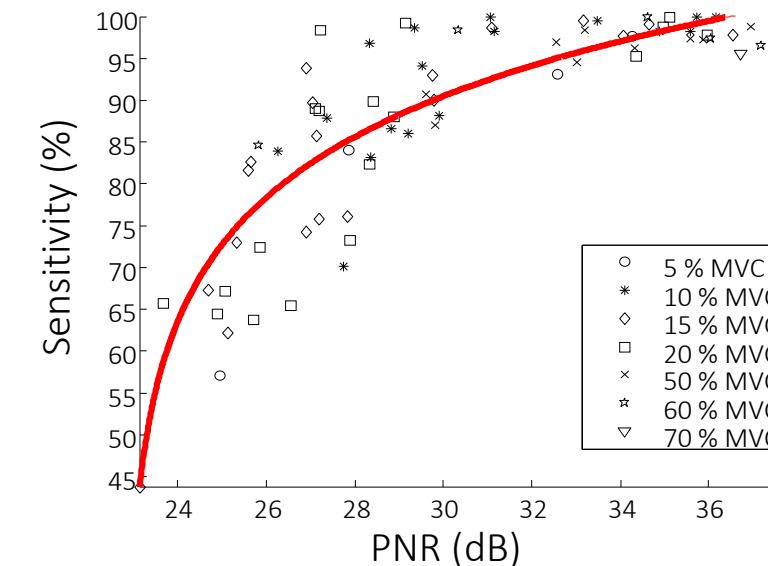
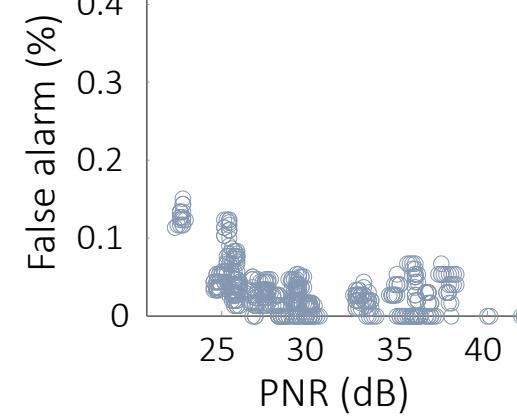
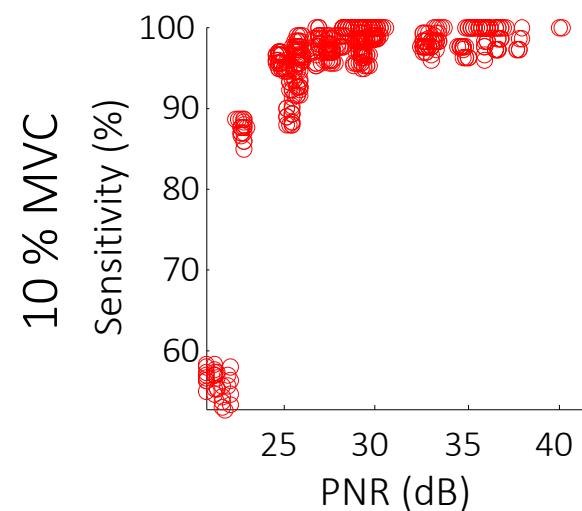
# BSS-based identification of MU firings



## Pulse-to-Noise Ratio (PNR):

- applied to EVERY identified motor unit
- no additional experimental costs
- reliable indicator of accuracy of motor unit identification

# Synthetic EMG, experimental surface & intramuscular EMG



Funded by  
the European Union

GA No. 101079392

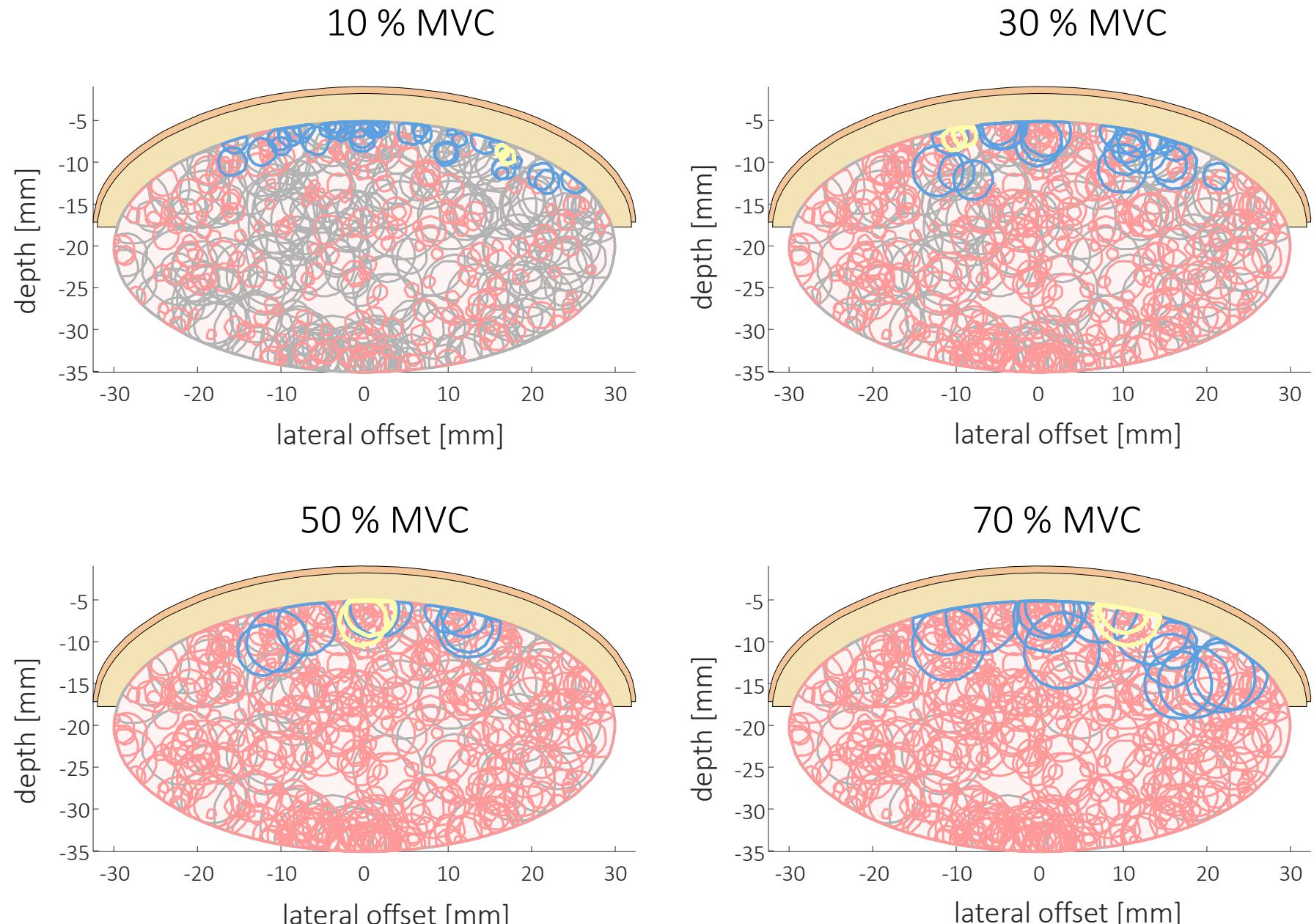


UK Research  
and Innovation

GA No. 10052152

# MU merging

Divjak et al. ICNR2020



Funded by  
the European Union

GA No. 101079392



UK Rese  
and Inn

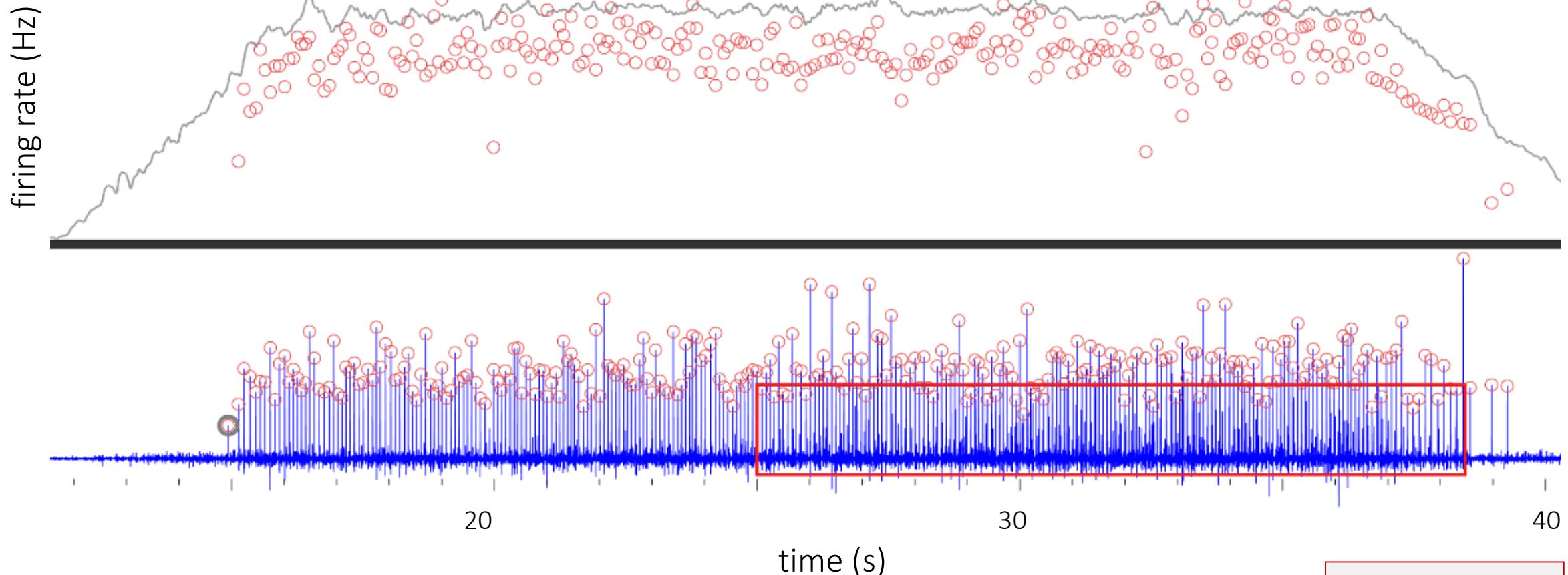
GA No. 100521

○ active MU

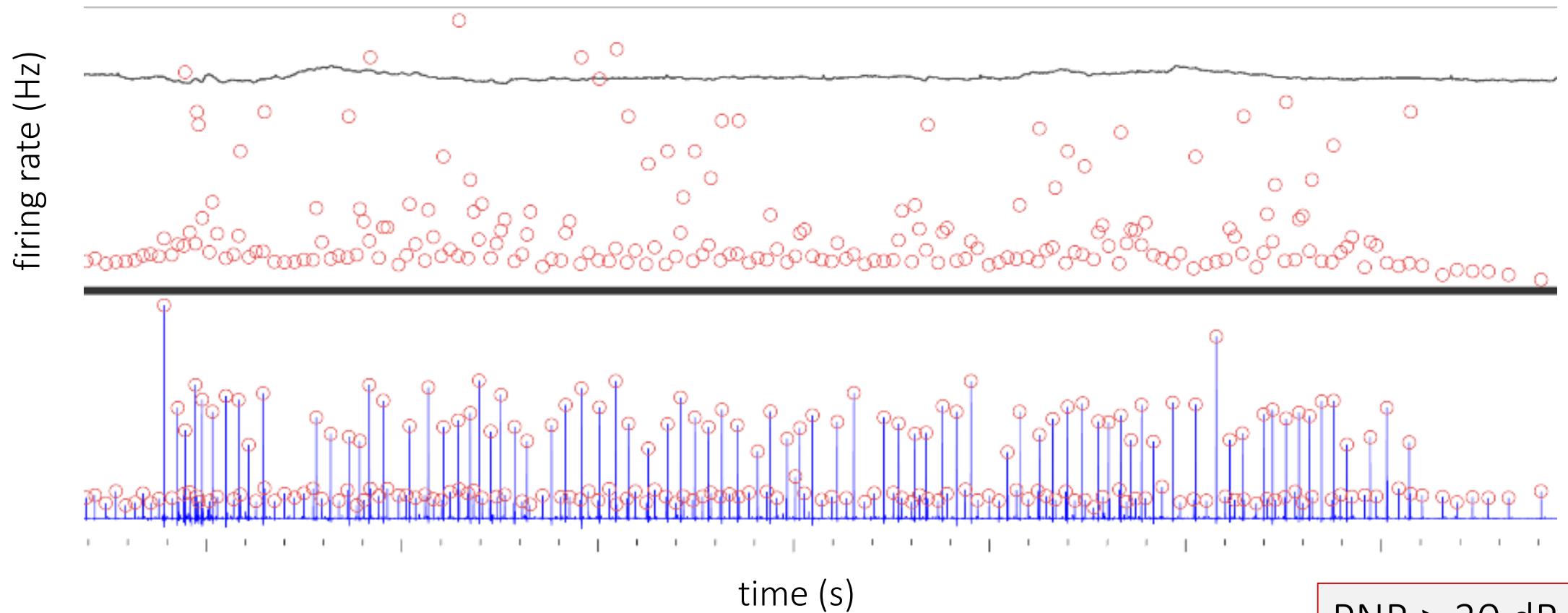
○ unmerged identified MU

○ merged identified MU

# MU merging, low $\text{CoV}_{\text{ISI}}$ is not enough



# MU merging, high PNR is not enough

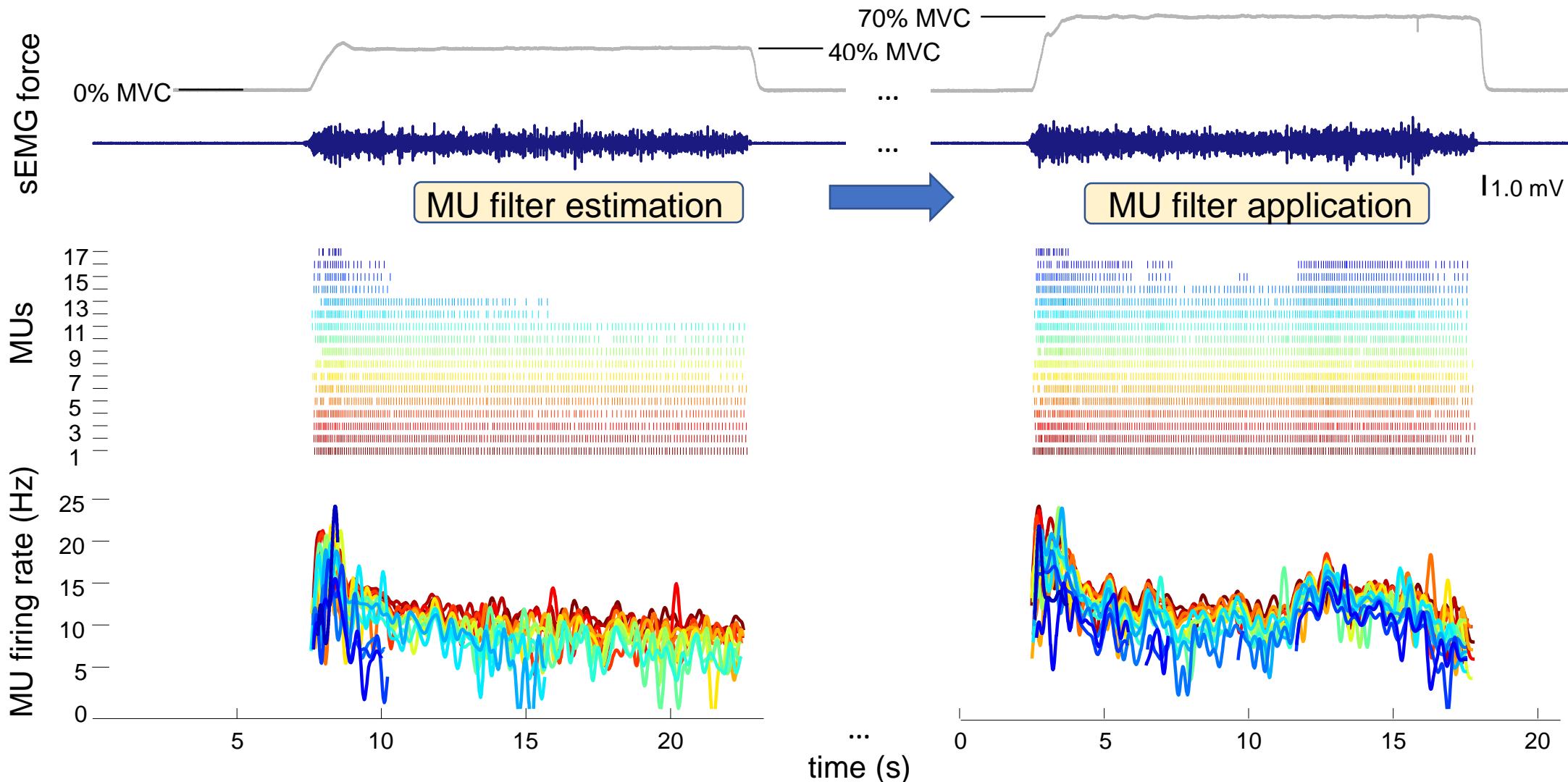


... but pathology plays with the regularity of MU firing.

$\text{PNR} > 30 \text{ dB}$   
 $\text{CoV}_{\text{ISI}} > 0.5$



# MU filter reused – pairwise comparisons



Funded by  
the European Union



UK Research  
and Innovation

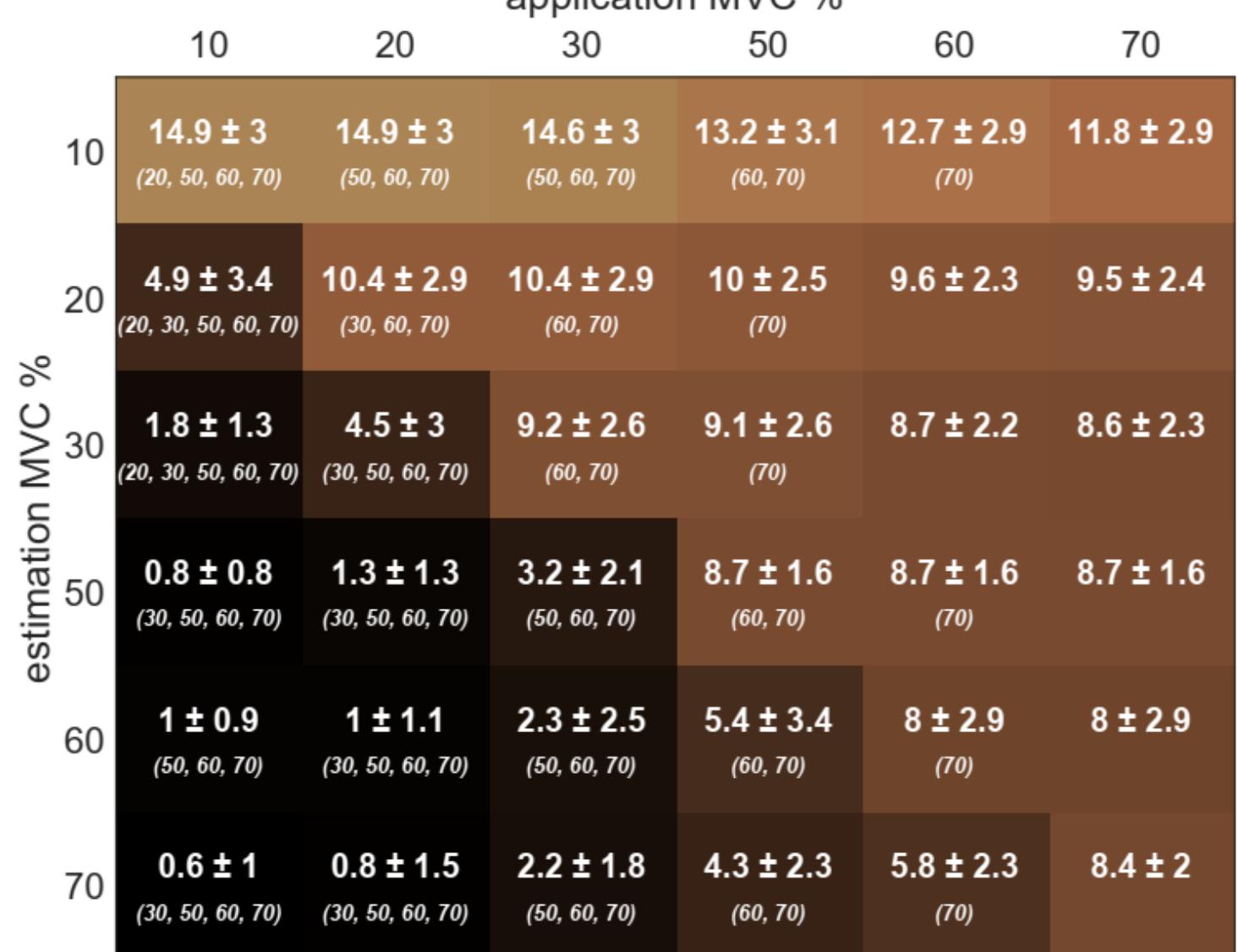
GA No. 101079392

GA No. 10052152

# EXAMPLE 1: MU tracking across different contraction levels

Frančič & Holobar, IEEE Access 2021

No. of tracked MUs  
Synthetic HDsEMG, SNR = 20 dB



# EXAMPLE 2: MU tracking across different contraction levels

Frančič & Holobar, IEEE Access 2021

Frequently, MUs  
cannot be tracked  
across conditions

Paired tests not  
possible

No. of tracked MUs  
Tibialis Anterior (TA)  
application MVC %

	10	20	30	50	60	70
10	<b><math>11.7 \pm 5.2</math></b> (20, 30, 50, 60, 70)	<b><math>6 \pm 4.8</math></b> (30, 50, 60, 70)	<b><math>3.1 \pm 4.5</math></b> (70)	<b><math>0.3 \pm 0.5</math></b>	<b><math>0.1 \pm 0.3</math></b>	<b><math>0.2 \pm 0.4</math></b>
20	<b><math>6.4 \pm 4.5</math></b> (20, 50, 60, 70)	<b><math>13.8 \pm 5.4</math></b> (30, 50, 60, 70)	<b><math>7.6 \pm 6.3</math></b> (50, 60, 70)	<b><math>1.8 \pm 2.8</math></b> (60, 70)	<b><math>0.2 \pm 0.4</math></b>	<b><math>0.1 \pm 0.3</math></b>
30	<b><math>4.8 \pm 4.6</math></b> (20, 30, 70)	<b><math>9.4 \pm 5.4</math></b> (30, 50, 60, 70)	<b><math>14.1 \pm 6</math></b> (50, 60, 70)	<b><math>3.7 \pm 3.4</math></b> (60, 70)	<b><math>1.1 \pm 1.5</math></b>	<b><math>0.2 \pm 0.7</math></b>
50	<b><math>2 \pm 3</math></b> (30, 50, 60)	<b><math>4.3 \pm 5.7</math></b> (30, 50, 60)	<b><math>8.8 \pm 5.9</math></b> (50, 70)	<b><math>17.2 \pm 6.4</math></b> (60, 70)	<b><math>8.9 \pm 5.9</math></b> (70)	<b><math>1.2 \pm 1.3</math></b>
60	<b><math>1 \pm 1.7</math></b> (30, 50, 60, 70)	<b><math>2.1 \pm 2.2</math></b> (30, 50, 60)	<b><math>5.7 \pm 3.1</math></b> (50, 60)	<b><math>14 \pm 5.3</math></b> (60, 70)	<b><math>16.9 \pm 6.7</math></b> (70)	<b><math>5.3 \pm 4.6</math></b>
70	<b><math>0.2 \pm 0.7</math></b> (20, 30, 50, 60, 70)	<b><math>0.2 \pm 0.7</math></b> (30, 50, 60, 70)	<b><math>1.6 \pm 1.7</math></b> (50, 60, 70)	<b><math>7.1 \pm 4</math></b> (60, 70)	<b><math>11 \pm 5.3</math></b> (70)	<b><math>13.8 \pm 4.7</math></b>



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152



# Simulated data

Full control of simulation parameters & grand truth known

**In Wilkinson notation:**

$\text{MaxDR} \sim 1 + \text{RecThr} + \text{RecDR} + (-1 + \text{RecThr} | \text{SubID}) + (-1 + \text{RecThr} | \text{ContRep}) + (-1 + \text{RecThr} | \text{SubID}: \text{MUid})$



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: Model in MATLAB



```
NoSubjects = 15; % play with the number of Subjects (e.g. NoSubjects = 5....)  
NoRepetitions = 3; % Number of contraction repetitions per subject  
NoMUs = 15; % play with the number of MUs (e.g. NoMUs = 5, NoMUs = 15....)  
portionOfMissedValues = 0.0; % portion of missed MUs (0 for 0%, 0.5 for 50 %)
```

## % FIXED FACTORS

```
C = 30; % maximum contraction level & intercept  
mean_recThSlope = -0.3; % mean slope of recruitment threshold factor  
mean_recDRSlope = -1; % mean slope of discharge rate factor  
recTh_recDR_interactionSlope = 0.0; % interaction between recruitment threshold  
and recruitment discharge rate
```

## % RANDOM FACTORS – UNIFORM DISTRIBUTION!!! (use randn for Normal distribution)

```
S = 0.2*(rand(1,NoSubjects) - 0.5); % random effect per subject  
R = 0.025* (rand(NoRepetitions,NoSubjects) - 0.5); % random effect per repetition  
M = 0.025* (rand(NoRepetitions,NoSubjects,NoMUs) - 0.5); % random effect per MU
```

# Simulated data: MATLAB script



```
for Si = 1:NoSubjects
    for Ri = 1>NoRepetitions
        for Mi = 1>NoMUs
            % two factors
            RecThr(end+1,1) = Mi/NoMUs*0.7*C+0.1*rand();
            RecDR(end+1,1) = 7+rand();

            % coefficients
            DRintercept(end+1,1) = C;
            recThSlope(end+1,1) = mean_recThSlope + S(1, Si) + R(Ri, Si) + M(Ri, Si, Mi);
            recDRSlope(end+1,1) = mean_recDRSlope;

            % MaxDR generation
            MaxDR(end+1,1) = DRintercept(end,1) + recDRSlope(end,1)*RecDR(end) +
                recThSlope(end,1)*RecThr(end) +
                recTh_recDR_interactionSlope*RecDR(end)*RecThr(end) + 0.5*randn(1);

        end
    end
end
```



Funded by  
the European Union

GA No. 101079392



UK Research  
and Innovation

GA No. 10052152

# Simulated data: MATLAB script



```
for Si = 1:NoSubjects  
    for Ri = 1>NoRepetitions  
        for Mi = 1>NoMUs
```

In Wilkinson notation (with some simplifications):

MaxDR ~ **1 + RecThr+RecDR+ (-1 + RecThr|SubID) + (-1 + RecThr|ContRep) + (-1 + RecThr|SubID:MUId)**

```
% coefficients  
DRintercept(end+1,1) = C;  
recThSlope(end+1,1) = mean_recThSlope + S(1,Si) + R(Ri,Si) + M(Ri,Si,Mi);  
recDRSlope(end+1,1) = mean_recDRSlope;  
  
% MaxDR generation  
MaxDR(end+1,1) = DRintercept(end,1) + recDRSlope(end,1)*RecDR(end) +  
recThSlope(end,1)*RecThr(end) +  
recTh_recDR_interactionSlope*RecDR(end)*RecThr(end) + 0.5*randn(1);  
end  
end  
end
```



↑  
residuals

Fixed effects/factors  
Random effects/factors



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Use MATLAB code to generate the simulated data: MATLAB script



Play with:

- number of subjects: **NoSubjects = 15**
- number of contraction repetitions: **NoRepetitions = 3**
- number of MUs: **NoMUs = 15;**
- portion of missed Mus: **portionOfMissedValues = 0.0**
- distribution of random factors: **S = 0.2\*(rand(1,NoSubjects) ...**
- standard deviation of residuals: **...+ 0.5\*randn(1)**

# Generated synthetic data



	SubID	ContRep	MUid	RecThr	RecDR	MaxDR
1	1	1	1	1.304582	7.809072	21.69751
2	1	1	2	2.217251	7.490311	21.89127
3	1	1	3	3.477377	7.564893	20.60219
4	1	1	4	5.111151	7.361645	20.87282
5	1	1	5	5.609156	7.127993	21.18084
6	1	1	6	7.242648	7.229332	20.36605
7	1	1	7	8.026397	7.187388	20.26364
8	1	1	8	9.160058	7.882963	18.96820
9	1	1	9	9.677212	7.819587	19.13943
10	1	1	10	10.832018	7.545053	18.73962
11	1	1	11	11.889022	7.700884	18.68902
12	1	1	12	13.502939	7.909991	17.93430
13	1	1	13	14.150664	7.329819	18.27405
14	1	1	14	14.736652	7.620602	17.36552
15	1	1	15	16.302724	7.746850	17.29255
16	1	1	16	16.922055	7.069719	16.69830
17	1	1	17	18.499537	7.925429	17.01645
18	1	1	18	19.771736	7.393052	15.97765
19	1	1	19	20.159837	7.010169	16.12223
20	1	1	20	21.240958	7.286717	15.67633
21	1	2	1	1.906525	7.028672	23.07511
22	1	2	2	2.485699	7.812762	21.07494
23	1	2	3	4.059424	7.664201	21.26823
24	1	2	4	5.058551	7.517004	20.18698
25	1	2	5	5.890015	7.920506	20.34778
26	1	2	6	7.178889	7.076835	19.80120

Showing 1 to 27 of 1,200 entries, 6 total columns



Funded by  
the European Union

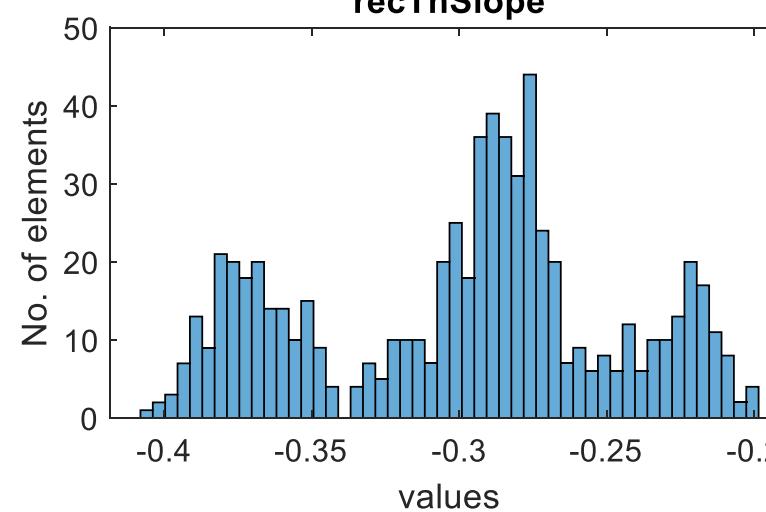
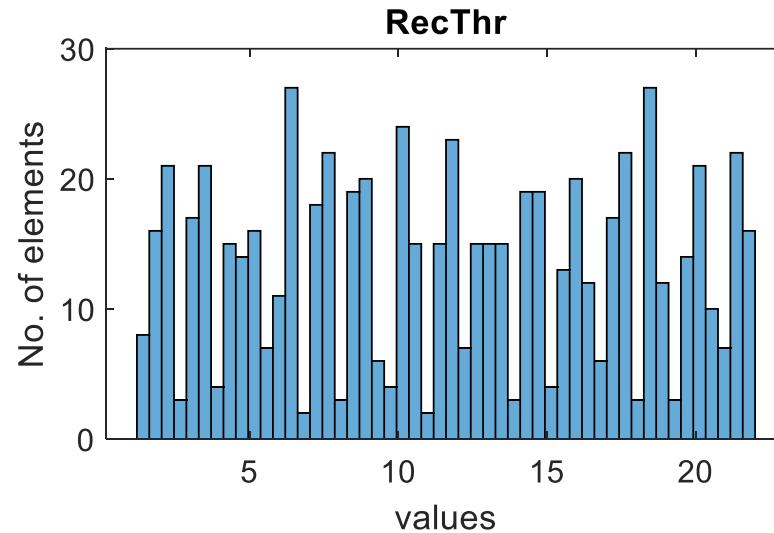
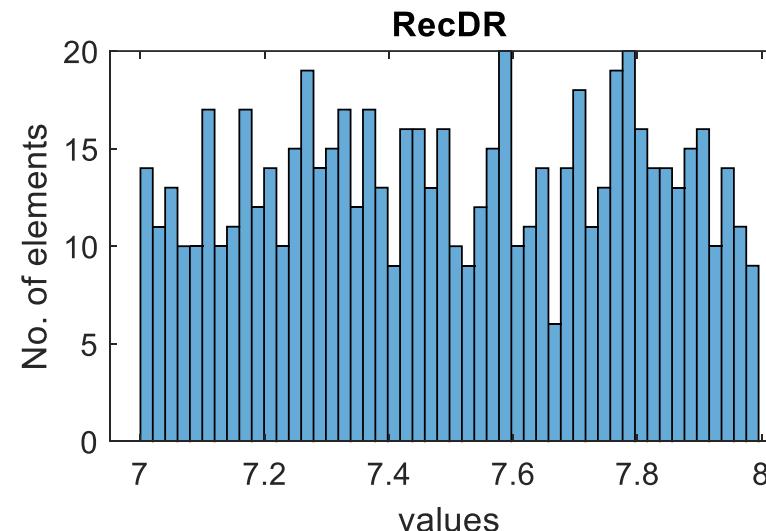
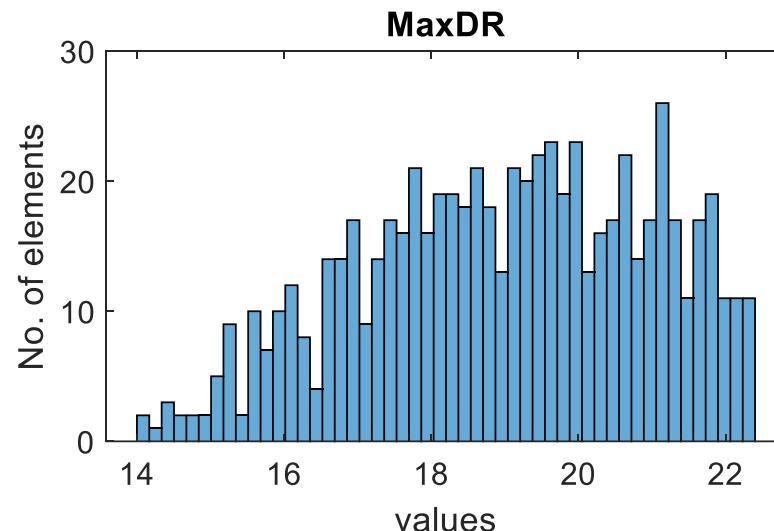


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: MATLAB script



Funded by  
the European Union

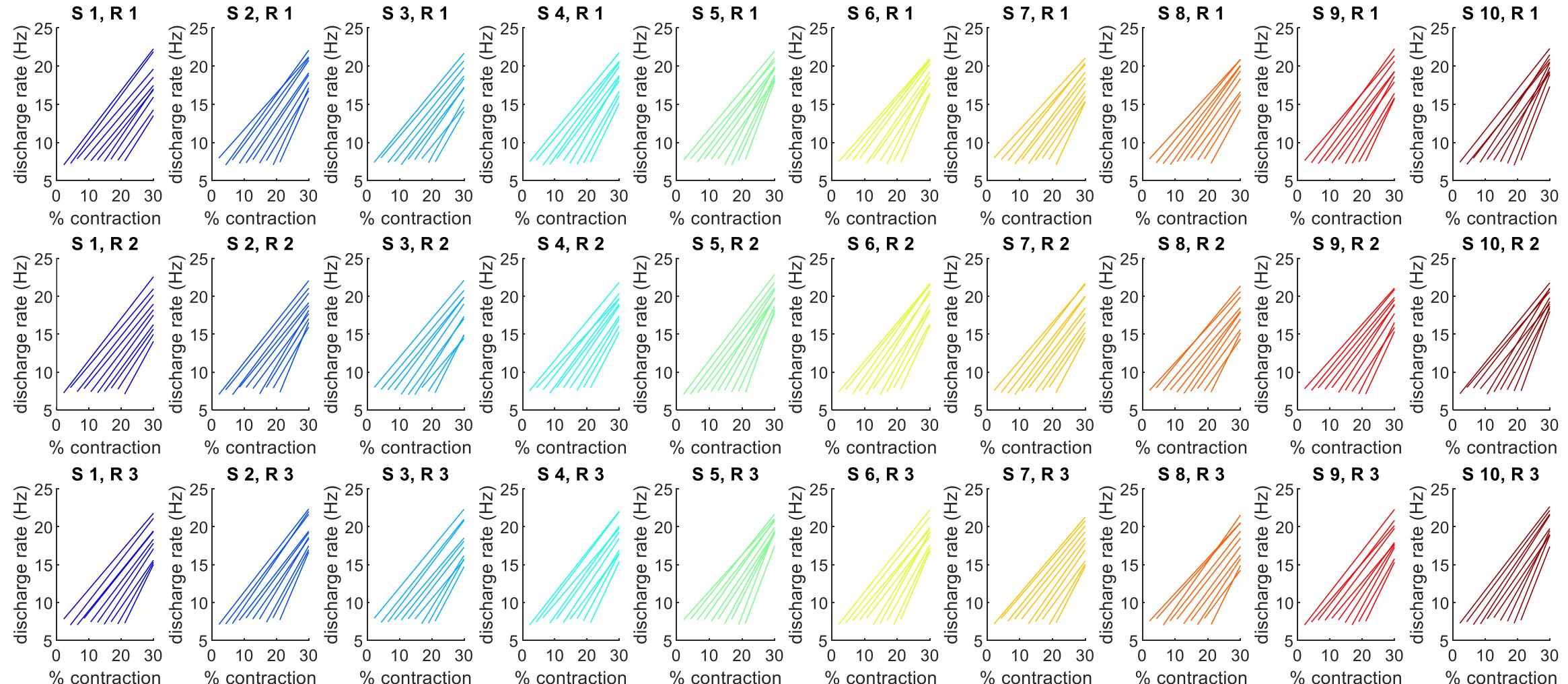


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data



Funded by  
the European Union

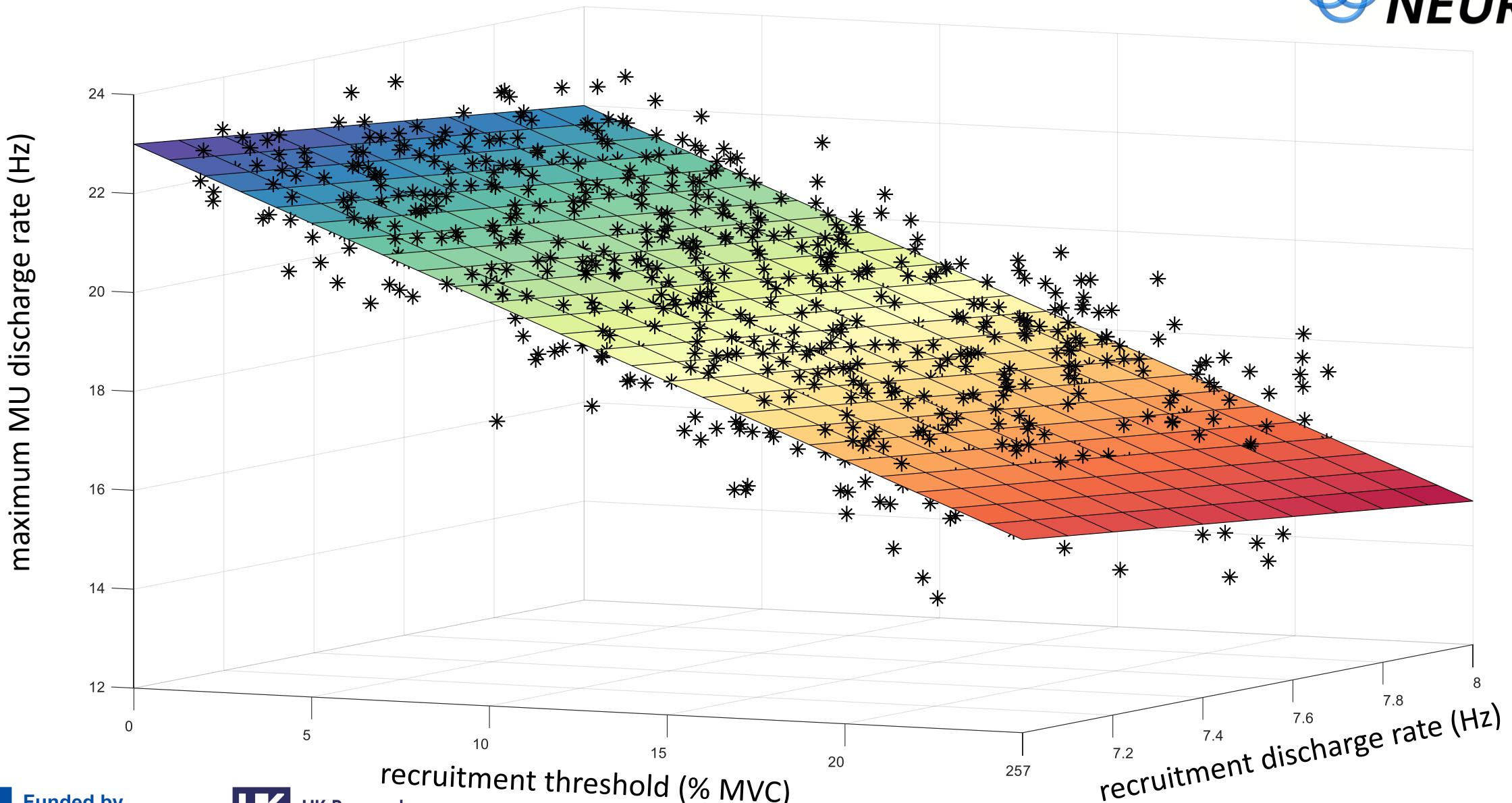


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: different LMEs



**MaxDR ~ 1 + RecThr + RecDR**

## Rstudio

```
lme2 <- lm(MaxDR ~ 1 + RecThr + RecDR, data = emg.data)
summary(lme2)

### plot residuals with qq-plot
qqnorm(residuals(lme2))
qqline(residuals(lme2))

### Visual check of model various assumptions
check_model(lme2)
```

## MATLAB

```
lme2 = fitlme(Table1,'MaxDR ~ 1 + RecThr + RecDR')

% Visual check of model various assumptions
figure; subplot(2,2,1); plotResiduals(lme2,'probability');
subplot(2,2,2); plotResiduals(lme2,'lagged');
subplot(2,2,3); plotResiduals(lme2,'histogram');
subplot(2,2,4); plotResiduals(lme2,'caseorder');
compare(lme1,lme2)
```



Funded by  
the European Union



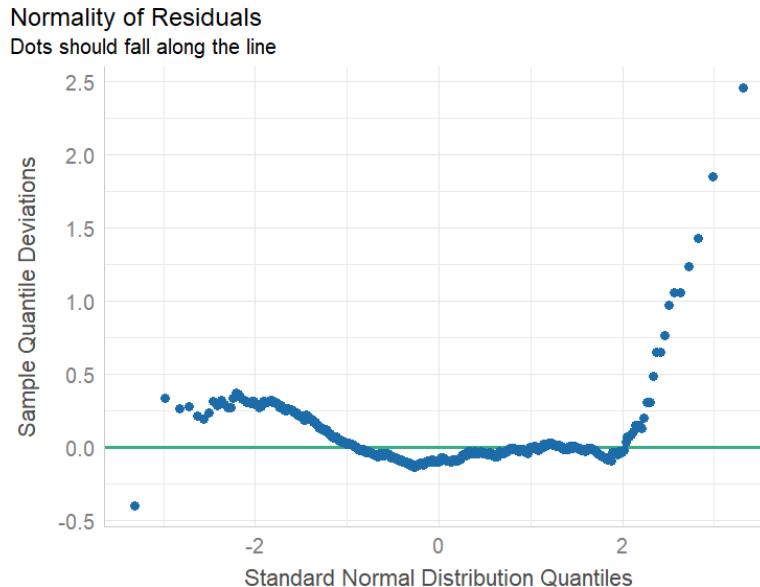
UK Research  
and Innovation

GA No. 101079392

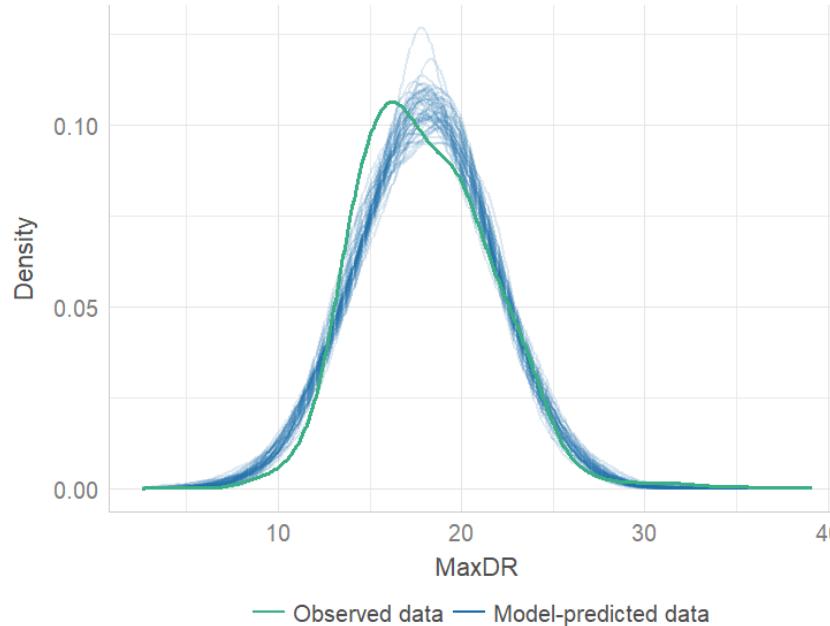
GA No. 10052152

# check\_model...

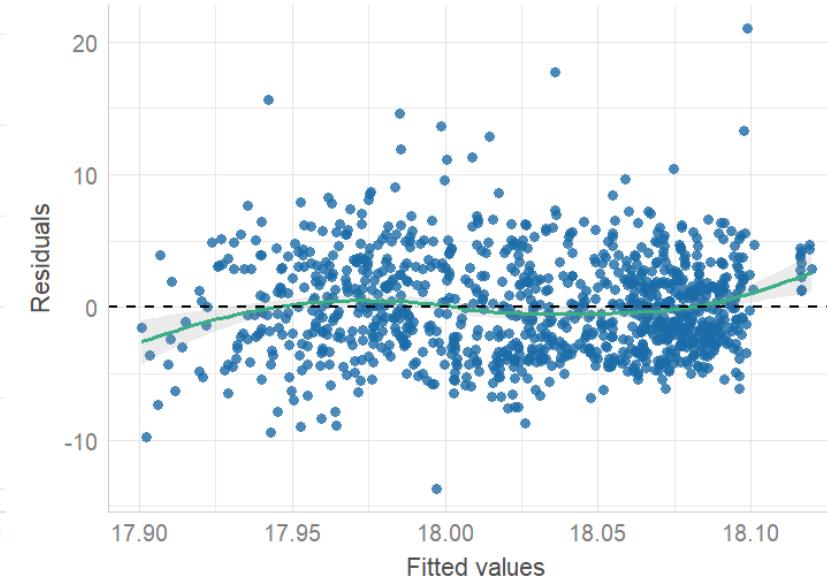
- normality of residuals
- normality of random effects
- heteroscedasticity
- homogeneity of variance
- multicollinearity



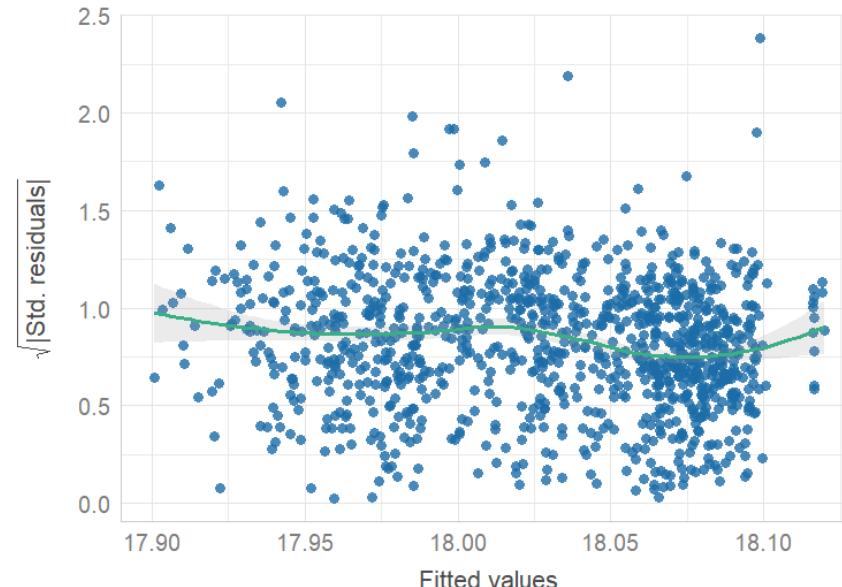
Posterior Predictive Check  
Model-predicted lines should resemble observed data line



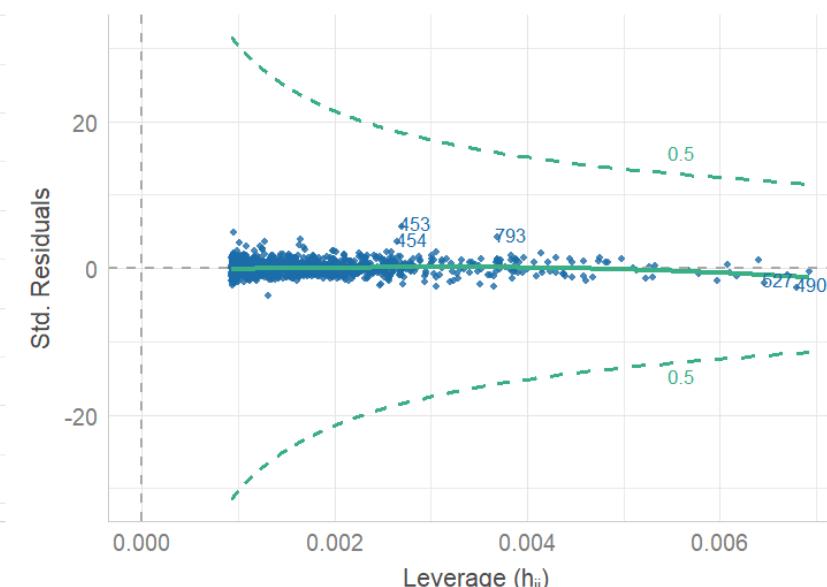
Linearity  
Reference line should be flat and horizontal



Homogeneity of Variance  
Reference line should be flat and horizontal



Influential Observations  
Points should be inside the contour lines



# Simulated data: different LMEs



**MaxDR ~ 1 + RecThr**

**Rstudio**

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	<b>22.500201</b>	<b>0.060776</b>	<b>370.21</b>	<2e-16 ***
RecThr	<b>-0.299514</b>	<b>0.004616</b>	<b>-64.89</b>	<2e-16 ***

**MATLAB**

Name	Estimate	SE	tStat	DF	pValue	Lower	Upper
{'(Intercept)'}	<b>22.5</b>	<b>0.060686</b>	<b>370.76</b>	673	0	22.381	22.619
{'RecThr'}	<b>-0.29951</b>	<b>0.0046091</b>	<b>-64.983</b>	673	3.3361e-292	-0.30856	-0.29046

**Ground truth:**

{'(Intercept)'}	<b>30.00</b>
{'RecThr'}	<b>-0.30</b>
{'RecDR'}	<b>-1.00</b>

**MaxDR ~ 1 + RecThr + RecDR**

**Rstudio**

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	<b>28.805324</b>	<b>0.704397</b>	<b>40.894</b>	<2e-16 ***
RecThr	<b>-0.300113</b>	<b>0.004365</b>	<b>-68.748</b>	<2e-16 ***
RecDR	<b>-0.839625</b>	<b>0.093489</b>	<b>-8.981</b>	<2e-16 ***

**MATLAB**

Name	Estimate	SE	tStat	DF	pValue	Lower	Upper
{'(Intercept)'}	<b>28.805</b>	<b>0.70283</b>	<b>40.985</b>	672	5.8802e-185	27.425	30.185
{'RecThr'}	<b>-0.30011</b>	<b>0.0043557</b>	<b>-68.901</b>	672	8.0329e-307	-0.30867	-0.29156
{'RecDR'}	<b>-0.83962</b>	<b>0.093281</b>	<b>-9.0011</b>	672	2.2713e-18	-1.0228	-0.65647



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: different LMEs in Rstudio



**MaxDR ~ 1 + RecThr + RecDR + (1 | ContRep) + (1 | SubID) + (1 | MUid)**

## Rstudio

	Estimate	Std. Error	df	t	value	Pr(> t )
(Intercept)	<b>30.085862</b>	<b>0.392933</b>	380.566120	76.57	<2e-16	***
RecThr	<b>-0.300210</b>	<b>0.002223</b>	660.004042	-135.04	<2e-16	***
RecDR	<b>-1.010187</b>	<b>0.048070</b>	660.204111	-21.02	<2e-16	***

## Ground truth:

{'(Intercept)'}	<b>30.00</b>
{'RecThr'}	<b>-0.30</b>
{'RecDR'}	<b>-1.00</b>

## MATLAB

Name	Estimate	SE	tStat	DF	pValue	Lower	Upper
{'(Intercept)'}	<b>30.086</b>	<b>0.39291</b>	76.572	672	0	29.314	30.857
{'RecThr'}	<b>-0.30021</b>	<b>0.0022231</b>	-135.04	672	0	-0.30458	-0.29585
{'RecDR'}	<b>-1.0102</b>	<b>0.048071</b>	-21.014	672	9.592e-76	-1.1046	-0.9158

**MaxDR ~ 1 + RecThr + RecDR + (RecThr | ContRep) + (RecThr | SubID) + (RecThr | MUid)**

## Rstudio

	Estimate	Std. Error	df	t	value	Pr(> t )
(Intercept)	<b>30.03710</b>	<b>0.16927</b>	654.57554	177.45	< 2e-16	***
RecThr	<b>-0.30053</b>	<b>0.01319</b>	15.67415	-22.78	1.95e-13	***
RecDR	<b>-1.00322</b>	<b>0.02243</b>	655.64726	-44.73	< 2e-16	***

## MATLAB

Name	Estimate	SE	tStat	DF	pValue	Lower	Upper
{'(Intercept)'}	<b>30.034</b>	<b>0.16931</b>	177.39	672	0	29.702	30.367
{'RecThr'}	<b>-0.3005</b>	<b>0.013158</b>	-22.837	672	7.012e-86	-0.32634	-0.27466
{'RecDR'}	<b>-1.0029</b>	<b>0.02246</b>	-44.652	672	2.936e-203	-1.047	-0.95879



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: Bayesian regression



**MaxDR ~ 1 + RecThr + RecDR**

## Rstudio

```
blr1 <- brm(MaxDR ~ RecThr+RecDR, data = emg.data,
               prior = c(set_prior("normal(0,3)", class = "b"),
                         set_prior("cauchy(0,2.5)", class = "sigma")),
               family = gaussian(), seed = 123123)

summary(blr1, waic = TRUE)
```

## MATLAB

```
NoPredictors=2;

PriorMd11 = bayeslm(NoPredictors,ModelType="diffuse", VarNames=["RecThr" "RecDR"]);
PriorMd11 = bayeslm(NoPredictors,ModelType="mixconjugateblm", VarNames=["RecThr" "RecDR"]);
plot(PriorMd11); set(gcf,'Position',get(0,'ScreenSize'))

X = Table1{Table1.ContLev==30 & Table1.PNR>PNRthreshold,PriorMd11.VarNames(2:end)};
y = Table1{Table1.ContLev==30 & Table1.PNR>PNRthreshold,"MaxDR"};
PosteriorMd11 = estimate(PriorMd11,X,y);
plot(PosteriorMd11,PriorMd11); set(gcf,'Position',get(0,'ScreenSize'))
```



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: Bayesian regression



`MaxDR ~ 1 + RecThr + RecDR`

`Rstudio`

Population-Level Effects:

	Estimate	Est.Error	l-95%	CI	u-95%	CI	Rhat	Bulk_ESS	Tail_ESS
Intercept	<b>28.80</b>	<b>0.71</b>	27.41		30.21	1.00	3666	2806	
RecThr	<b>-0.30</b>	<b>0.00</b>	-0.31		-0.29	1.00	5574	3248	
RecDR	<b>-0.84</b>	<b>0.09</b>	-1.03		-0.65	1.00	3656	2727	

Converged or not?



Family Specific Parameters:

	Estimate	Est.Error	l-95%	CI	u-95%	CI	Rhat	Bulk_ESS	Tail_ESS
sigma	<b>0.69</b>	<b>0.02</b>	0.65		0.72	1.00	3745	3395	

`MATLAB`

	Mean	Std	CI95	Positive	Distribution	Regime
<hr/>						
Intercept	<b>28.2943</b>	<b>0.6873</b>	[26.942, 29.637]	1.000	Empirical	1
RecThr	<b>-0.2999</b>	<b>0.0044</b>	[-0.308, -0.291]	0.000	Empirical	1
RecDR	<b>-0.7720</b>	<b>0.0912</b>	[-0.950, -0.592]	0.000	Empirical	1
Sigma2	<b>0.4707</b>	<b>0.0259</b>	[ 0.422, 0.524]	1.000	Empirical	NaN

**Ground truth:**

{'(Intercept)'}	<b>30.00</b>
{'RecThr'}	<b>-0.30</b>
{'RecDR'}	<b>-1.00</b>



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: Bayesian regression



**MaxDR ~ 1 + RecThr + RecDR + ContRep SubID + MUid**

## Rstudio

Population-Level Effects:

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
Intercept	<b>29.51</b>	<b>0.66</b>	28.20	30.81	1.00	3889	2832
RecThr	<b>-0.29</b>	<b>0.09</b>	-0.46	-0.12	1.00	2246	2293
RecDR	<b>-0.88</b>	<b>0.09</b>	-1.05	-0.70	1.00	3941	2635
SubID	<b>-0.06</b>	<b>0.01</b>	-0.07	-0.05	1.00	4695	2770
ContRep	<b>0.02</b>	<b>0.03</b>	-0.04	0.08	1.00	4041	2858
MUid	<b>-0.01</b>	<b>0.12</b>	-0.26	0.22	1.00	2241	2351

**Ground truth:**

{'(Intercept)'}	<b>30.00</b>
{'RecThr'}	<b>-0.30</b>
{'RecDR'}	<b>-1.00</b>

Family Specific Parameters:

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
sigma	0.64	0.02	0.61	0.68	1.00	3778	2491

## MATLAB

	Mean	Std	CI95	Positive	Distribution
<hr/>					
Intercept	<b>29.5166</b>	<b>0.6693</b>	[28.204, 30.829]	1.000	t (29.52, 0.67^2, 6.7e+02)
RecThr	<b>-0.2917</b>	<b>0.0877</b>	[-0.464, -0.120]	0.000	t (-0.29, 0.09^2, 6.7e+02)
RecDR	<b>-0.8795</b>	<b>0.0877</b>	[-1.051, -0.707]	0.000	t (-0.88, 0.09^2, 6.7e+02)
SubID	<b>-0.0567</b>	<b>0.0057</b>	[-0.068, -0.045]	0.000	t (-0.06, 0.01^2, 6.7e+02)
ContRep	<b>0.0185</b>	<b>0.0303</b>	[-0.041, 0.078]	0.730	t (0.02, 0.03^2, 6.7e+02)
MUid	<b>-0.0118</b>	<b>0.1227</b>	[-0.252, 0.229]	0.462	t (-0.01, 0.12^2, 6.7e+02)
Sigma2	0.4124	0.0226	[ 0.370, 0.459]	1.000	IG(334.50, 0.0073)



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data: Bayesian regression



```
MaxDR ~ 1 + RecThr+RecDR+ (-1 + RecThr|ContRep) + (-1 + RecThr|SubID) + (-1 + RecThr|MUid)
```

## Rstudio

Group-Level Effects:

~**ContRep** (Number of levels: 3)

	Estimate	Est.Error	l-95%	CI	u-95%	CI	Rhat	Bulk_ESS	Tail_ESS
--	----------	-----------	-------	----	-------	----	------	----------	----------

<b>sd(RecThr)</b>	0.01	0.02	0.00	0.04	1.01	592	1301		
-------------------	------	------	------	------	------	-----	------	--	--

~**MUid** (Number of levels: 15)

	Estimate	Est.Error	l-95%	CI	u-95%	CI	Rhat	Bulk_ESS	Tail_ESS
--	----------	-----------	-------	----	-------	----	------	----------	----------

<b>sd(RecThr)</b>	0.00	0.00	0.00	0.00	1.01	423	371		
-------------------	------	------	------	------	------	-----	-----	--	--

~**SubID** (Number of levels: 15)

	Estimate	Est.Error	l-95%	CI	u-95%	CI	Rhat	Bulk_ESS	Tail_ESS
--	----------	-----------	-------	----	-------	----	------	----------	----------

<b>sd(RecThr)</b>	0.06	0.01	0.04	0.09	1.06	55	460		
-------------------	------	------	------	------	------	----	-----	--	--

Population-Level Effects:

	Estimate	Est.Error	l-95%	CI	u-95%	CI	Rhat	Bulk_ESS	Tail_ESS
--	----------	-----------	-------	----	-------	----	------	----------	----------

<b>Intercept</b>	<b>30.03</b>	<b>0.18</b>	29.68	30.37	1.02	392	1278		
------------------	--------------	-------------	-------	-------	------	-----	------	--	--

<b>RecThr</b>	<b>-0.30</b>	<b>0.02</b>	-0.33	-0.27	1.04	130	374		
---------------	--------------	-------------	-------	-------	------	-----	-----	--	--

<b>RecDR</b>	<b>-1.00</b>	<b>0.02</b>	-1.05	-0.96	1.02	330	1178		
--------------	--------------	-------------	-------	-------	------	-----	------	--	--

Family Specific Parameters:

	Estimate	Est.Error	l-95%	CI	u-95%	CI	Rhat	Bulk_ESS	Tail_ESS
--	----------	-----------	-------	----	-------	----	------	----------	----------

<b>sigma</b>	0.16	0.00	0.15	0.17	1.02	249	834		
--------------	------	------	------	------	------	-----	-----	--	--

## Ground truth:

{'Intercept'}	<b>30.00</b>
---------------	--------------

{'RecThr'}	<b>-0.30</b>
------------	--------------

{'RecDR'}	<b>-1.00</b>
-----------	--------------

## MATLAB

Model not supported



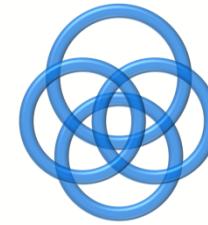
Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152



HYBRID  
**NEURO**

# Experimental data

Tibialis anterior, healthy subjects, 30% ramp contractions



Funded by  
the European Union



UK  
RI  
UK Research  
and Innovation

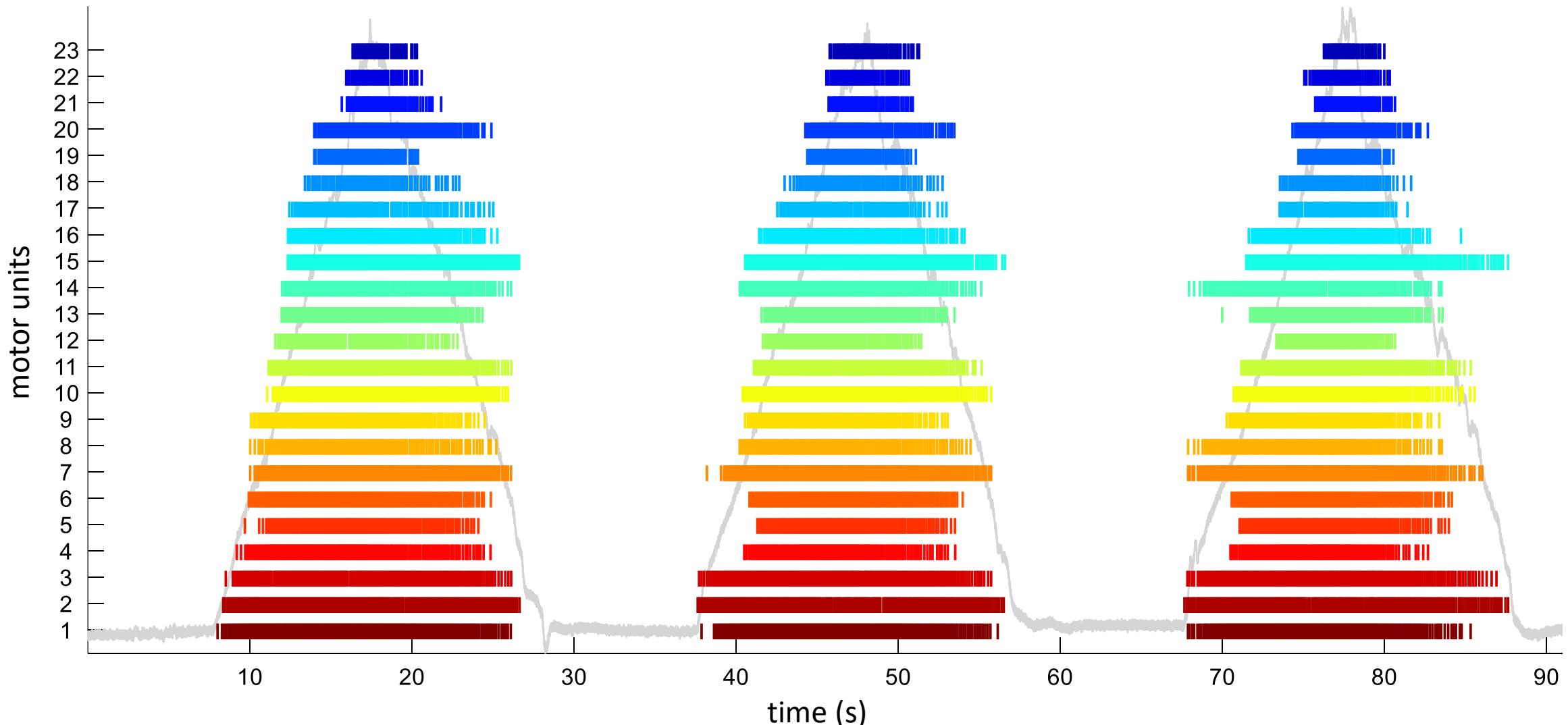
GA No. 101079392

GA No. 10052152

# Experimental data

- 19 healthy subjects
- Tibialis anterior muscle
- HDEMG signals
  - 64 channels
  - Sampling: 16 bit resolution and 2048 Hz of sampling rate
- Decomposition
  - Convolution Kernel Compensation (CKC)
  - Manually edited by two experts, only accurately identified motor units (MU) kept for analysis

# Experimental data: MU tracked across contractions, variations in MU recruitment threshold



Funded by  
the European Union

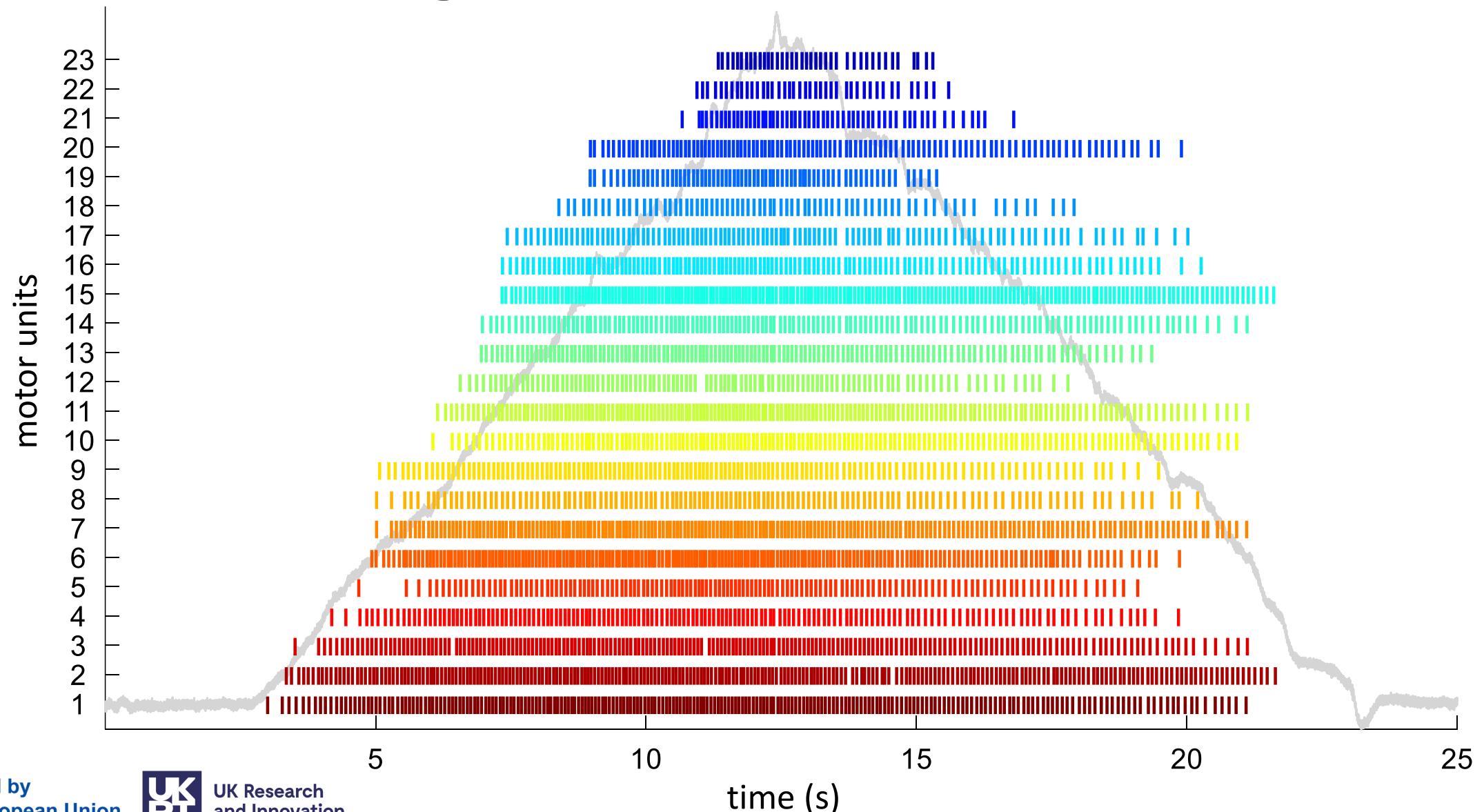


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Experimental data: variability of MU recruitment discharge rate



Funded by  
the European Union

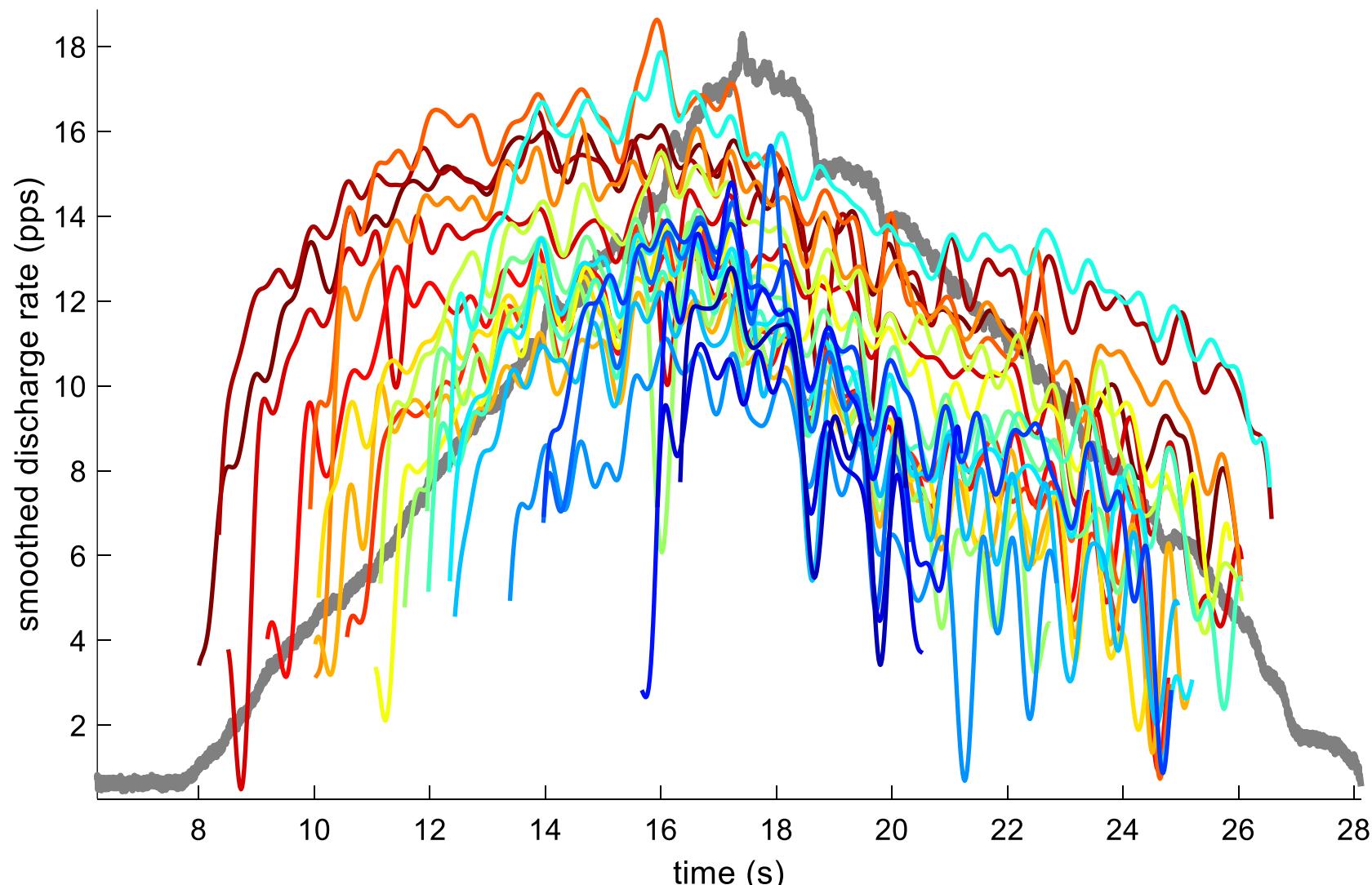


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Experimental data



Funded by  
the European Union

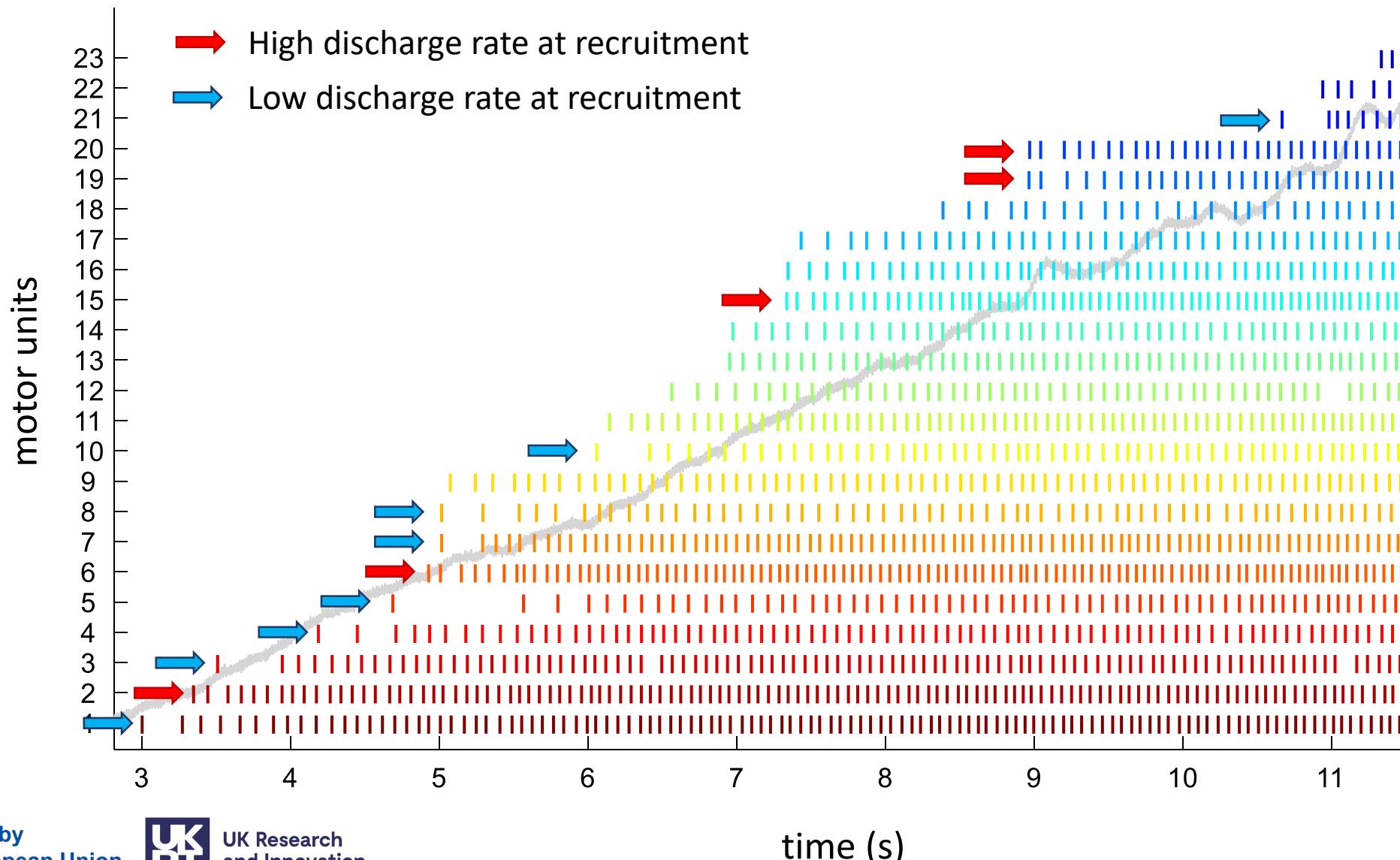


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Experimental data: variability of MU recruitment discharge rate



Funded by  
the European Union

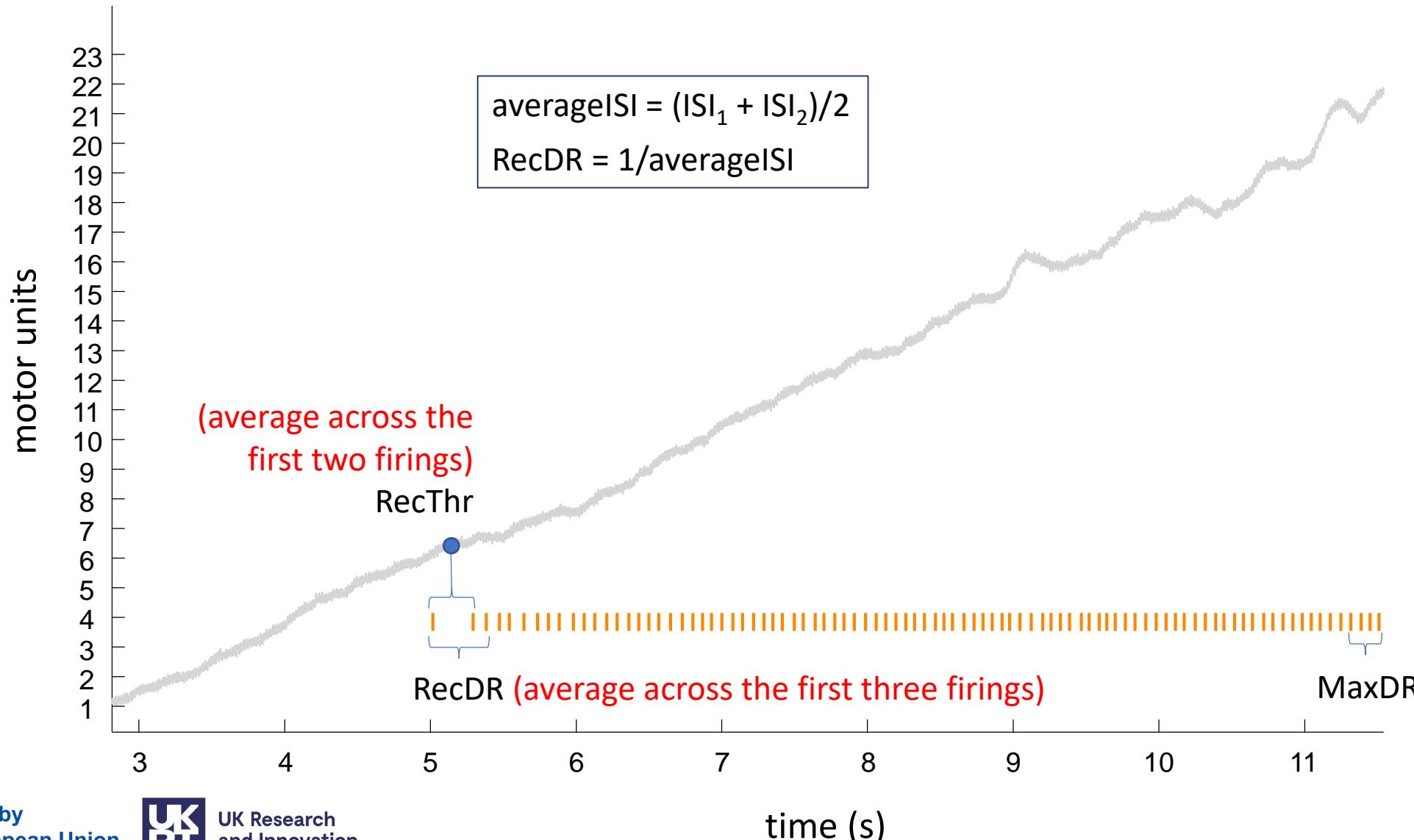


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Experimental data: discharge rate and recruitment threshold calculations



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Extracted data from experimental HDEMG

▲	SubID	ContLev	ContRep	MUid	RecThr	RecDR	MaxDR	PNR
1	1	30	1	1	0.6569055	7.335337	16.341819	25.91926
2	1	30	1	2	1.2383117	6.933358	15.925919	34.64867
3	1	30	1	4	1.9663557	10.367114	16.429530	31.07783
4	1	30	1	5	2.2390207	6.711693	15.387350	33.61697
5	1	30	1	7	3.8457452	7.212698	18.038826	33.71810
6	1	30	1	8	3.8825443	5.421191	14.658741	38.74707
7	1	30	1	9	3.9298414	5.149425	13.334769	39.86485
8	1	30	1	10	4.0012238	8.989763	15.940111	30.63242
9	1	30	1	11	4.3347160	6.607963	13.761101	34.93147
10	1	30	1	12	5.6329045	7.506767	13.223399	34.20745
11	1	30	1	15	9.4745756	7.632033	15.508550	30.69901
12	1	30	1	16	9.8373421	7.623913	14.182222	35.78660
13	1	30	1	17	9.9524461	7.566303	14.236357	33.57780
14	1	30	1	18	9.9524461	6.939700	14.002998	26.22607
15	1	30	1	19	9.9855810	8.212448	16.460278	33.74459
16	1	30	1	20	10.5830719	7.531014	13.934777	29.21554
17	1	30	1	21	11.5181735	7.383080	14.850754	25.98349
18	1	30	1	22	11.9682065	9.002758	12.781504	29.92432
19	1	30	1	23	12.2822505	5.789410	11.277619	34.08185
20	1	30	1	24	15.5528515	7.055209	14.593718	28.18759
21	1	30	1	25	15.5579976	4.528634	12.954859	27.72613
22	1	30	1	26	15.9778303	6.594490	13.636291	39.86824
23	1	30	1	27	15.9947253	9.981402	16.909188	27.32570
24	1	30	1	28	21.3873306	10.284329	14.310285	34.51161
25	1	30	2	1	0.2818675	8.765103	16.838501	25.24965
26	1	30	2	2	1.3257065	8.308624	12.678760	34.25484
27	1	30	2	4	2.2317743	9.353130	16.550371	28.55214
28	1	30	2	5	0.7520789	7.210378	15.319340	33.70748
29	1	30	2	6	0.0613727	0.970025	16.724040	26.22295

Showing 1 to 29 of 1,071 entries, 8 total columns



GA No. 101079392

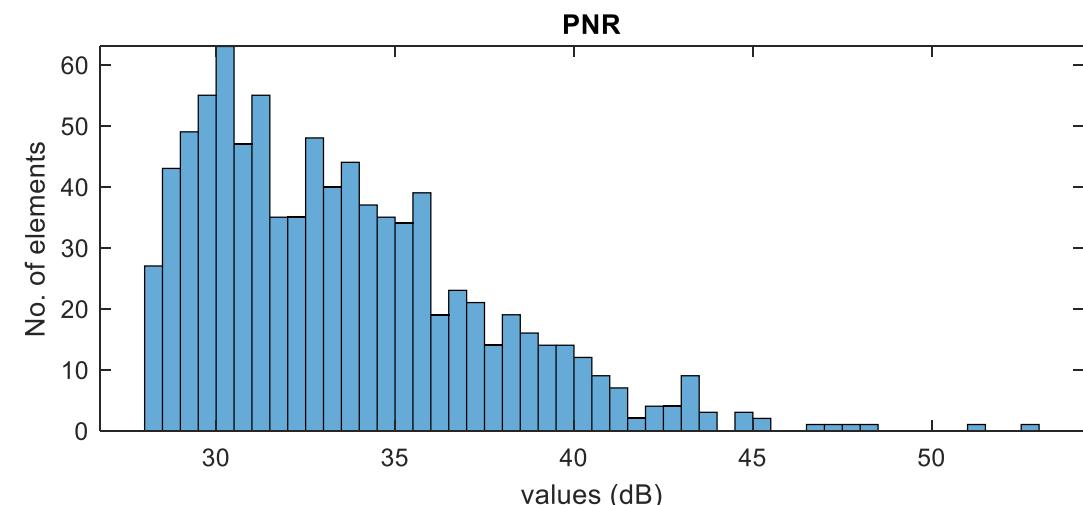
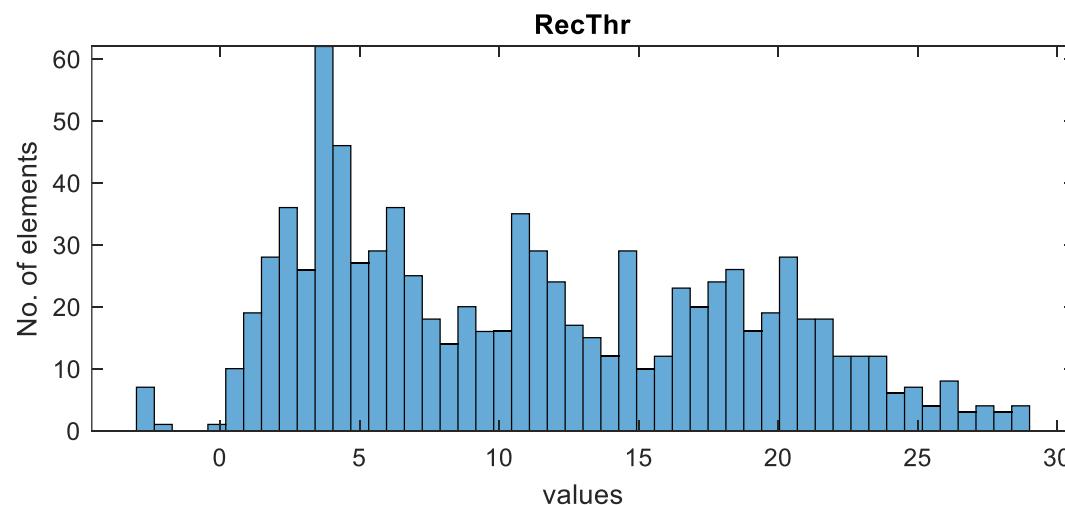
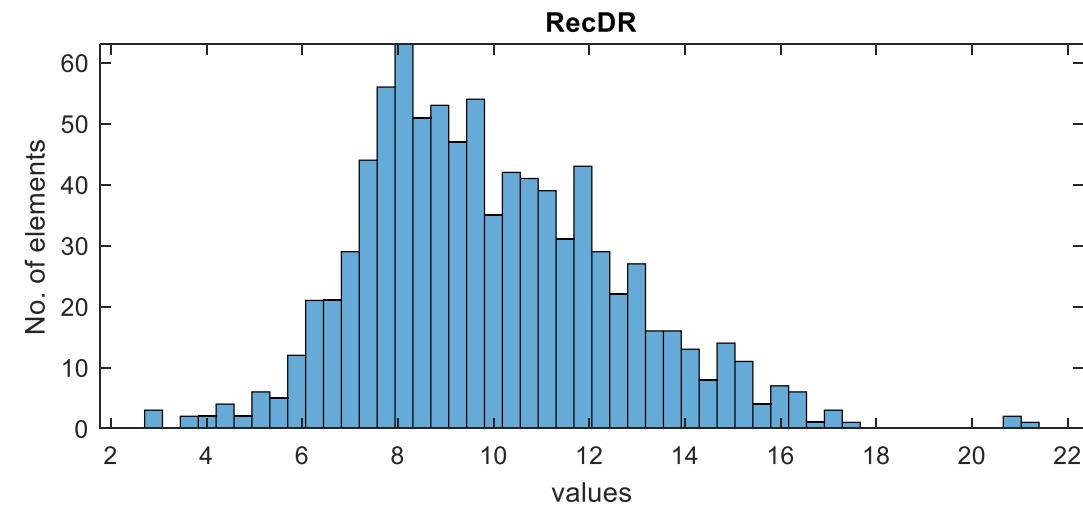
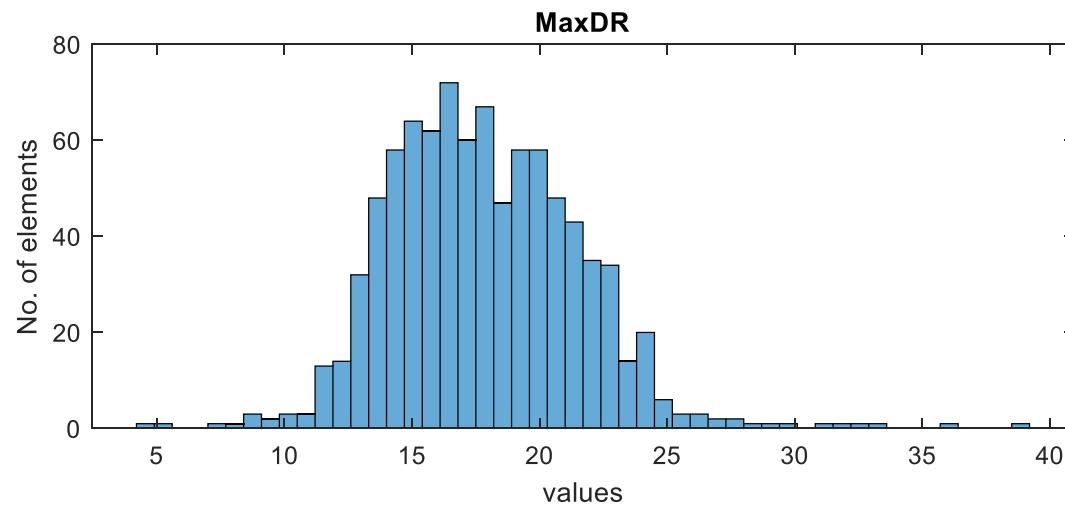
Funded by  
the European Union



UK Research  
and Innovation

GA No. 10052152

# Extracted data distributions



Funded by  
the European Union

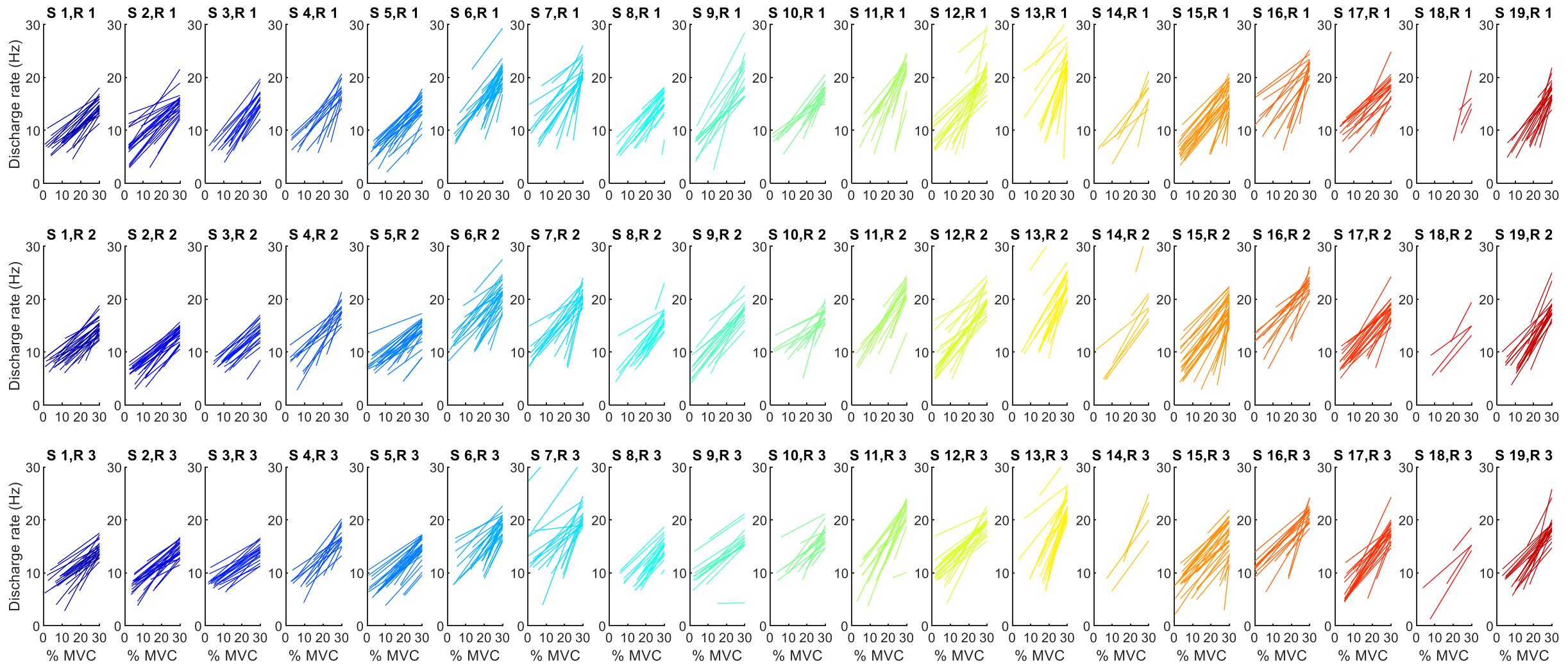


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Experimental data



Funded by  
the European Union

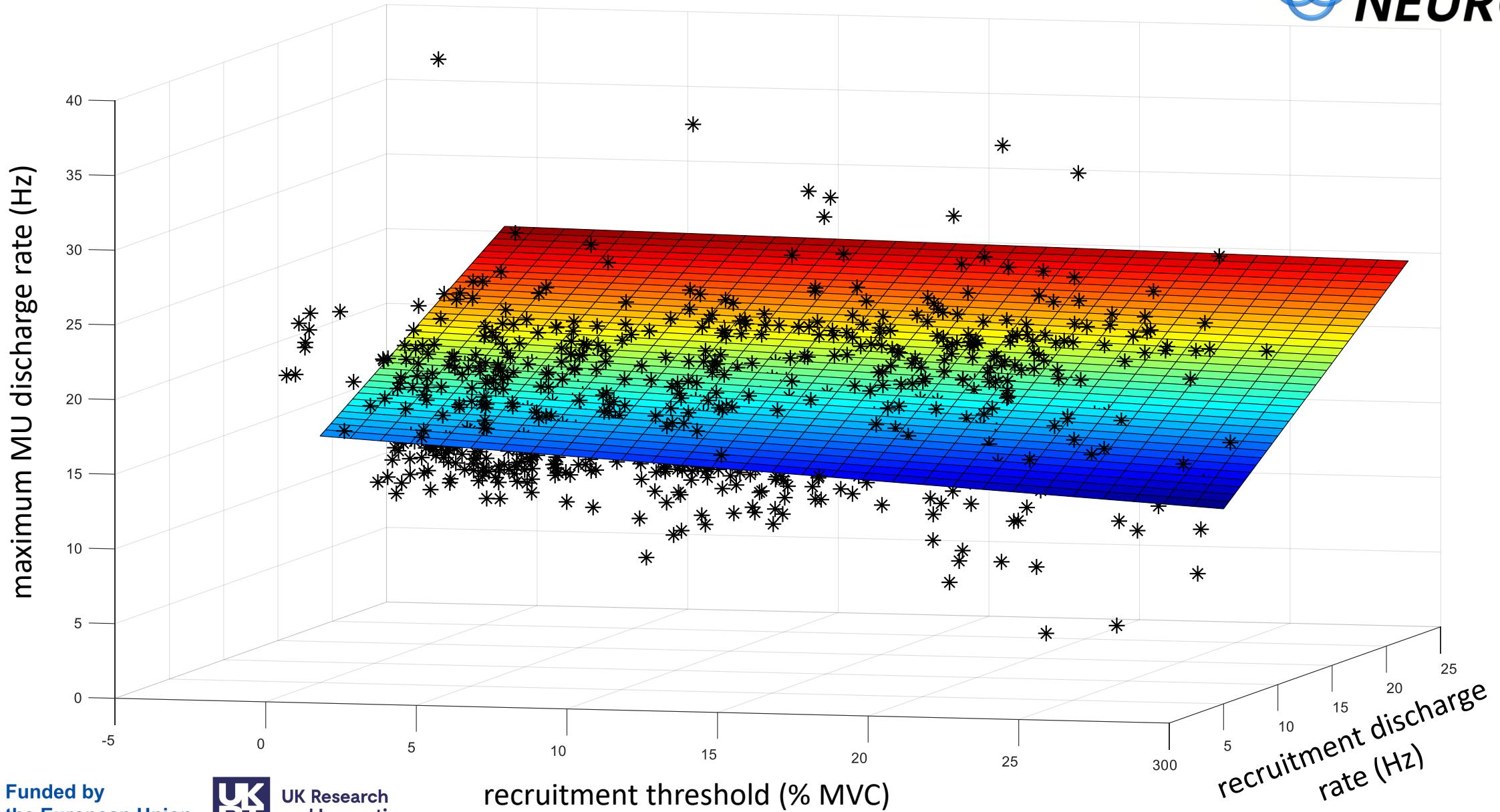


UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Simulated data



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Experimental data: different LMEs in MATLAB

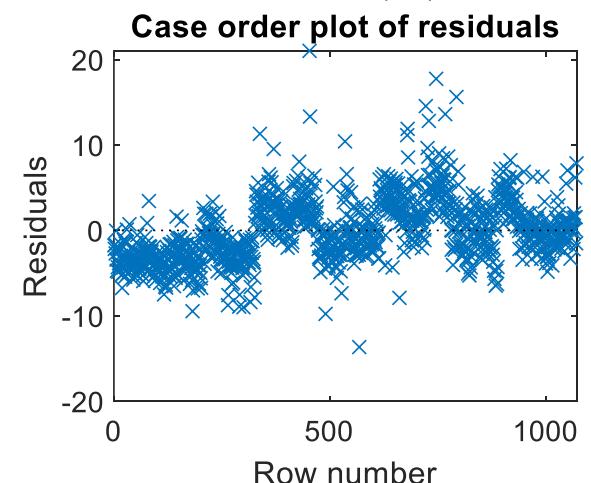
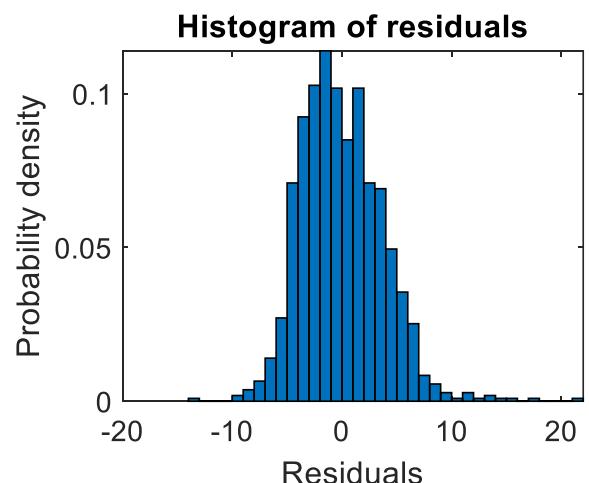
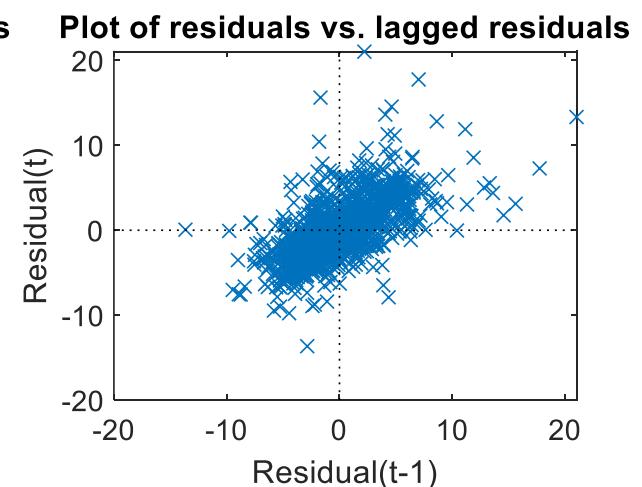
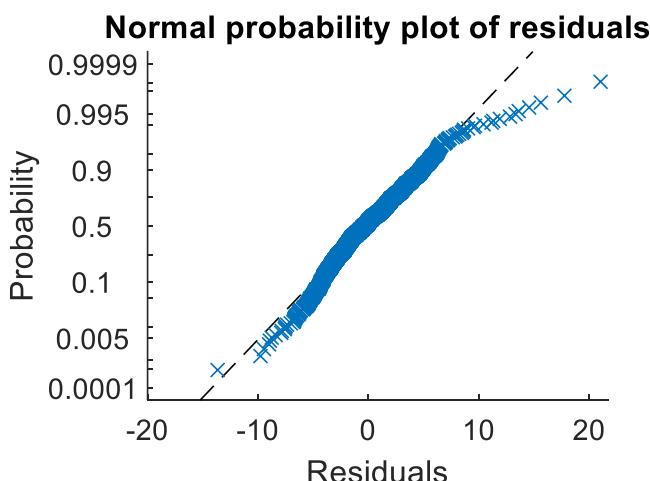


MaxDR ~ MaxDR ~ 1 + RecThr

## MATLAB

Name	Estimate	SE	tStat	DF	pValue	Lower	Upper
{'(Intercept)'}	18.1	0.19524	92.707	1069	0	17.717	18.483
{'RecThr'}	-0.0069234	0.015477	-0.44734	1069	0.65472	-0.037292	0.023445

Ground truth unknown!



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Experimental data: different LMEs in Rstudio

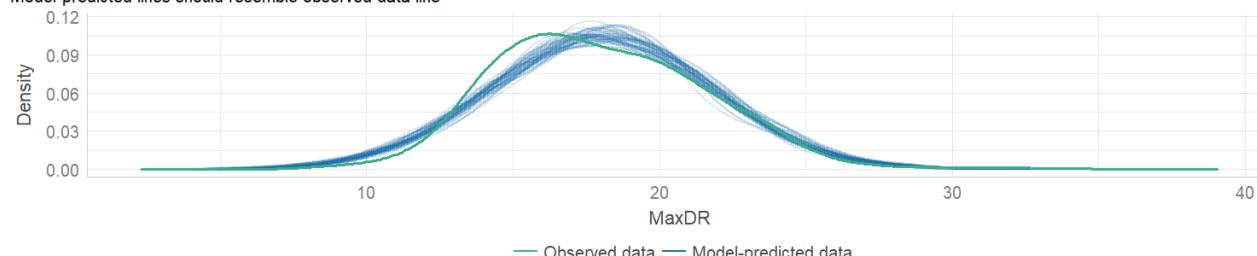


MaxDR ~ MaxDR ~ 1 + RecThr

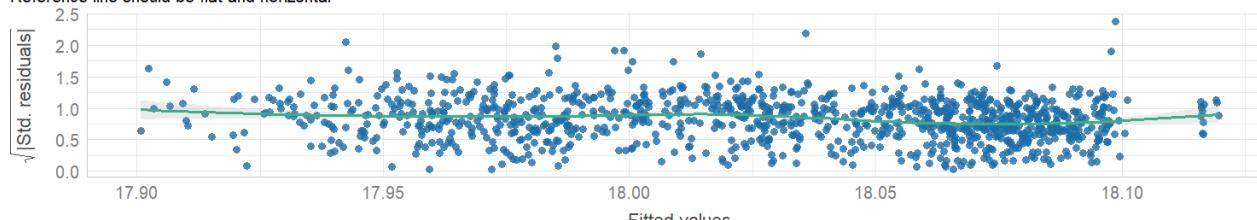
Rstudio

Coefficients:	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	18.100383	0.195426	92.620	<2e-16 ***
RecThr	-0.006923	0.015491	-0.447	0.655

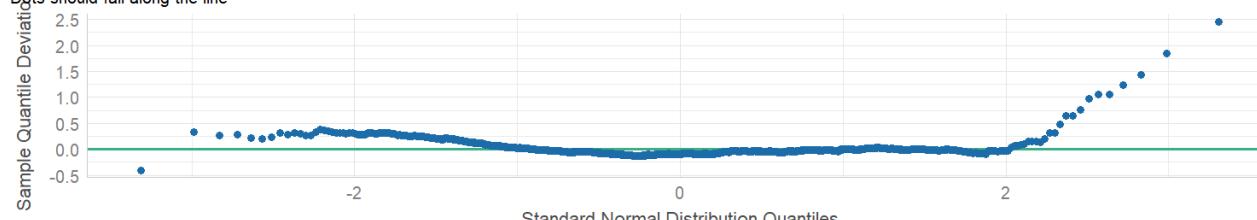
Posterior Predictive Check  
Model-predicted lines should resemble observed data line



Homogeneity of Variance  
Reference line should be flat and horizontal

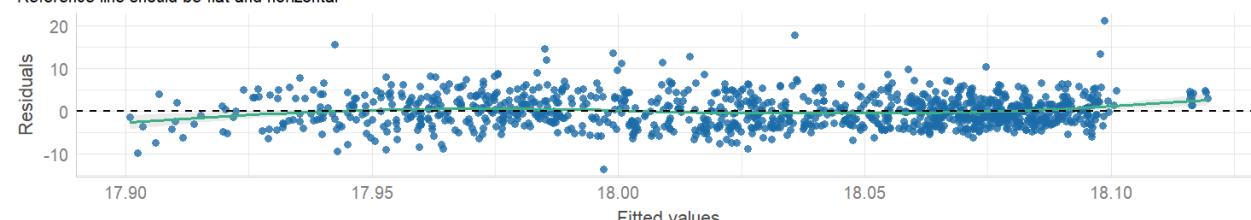


Normality of Residuals  
Dots should fall along the line

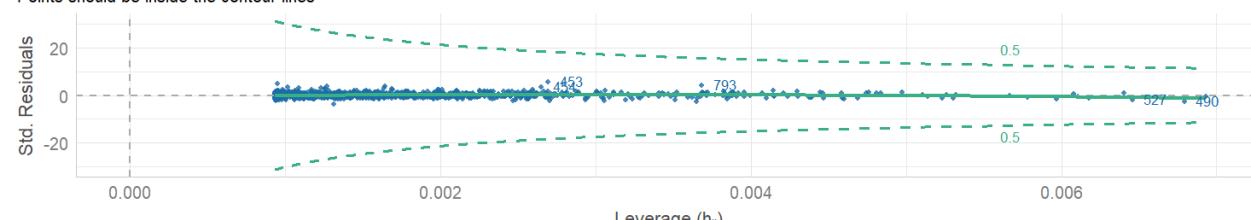


Ground truth unknown!

Linearity  
Reference line should be flat and horizontal



Influential Observations  
Points should be inside the contour lines



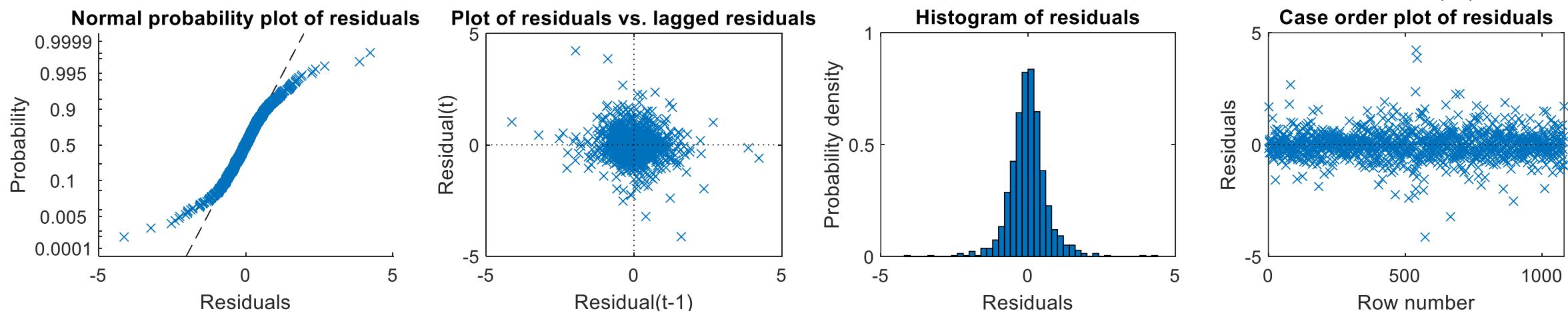
# Experimental data: different LMEs in MATLAB



```
MaxDR ~ 1 + RecThr*RecDR+(-1 + RecThr|ContRep) + (-1 + RecThr|SubID)+ ' ...  
' (-1 + RecThr|SubID:MUid) +(-1 + RecDR|ContRep) + (-1 + RecDR|SubID)+ (-1 + RecDR|SubID:MUid)
```

## MATLAB

Name	Estimate	SE	tStat	DF	pValue	Lower	Upper
{ '(Intercept)' }	<b>15.996</b>	<b>0.3341</b>	47.878	1067	<b>5.5495e-268</b>	15.34	16.652
{ 'RecThr' }	0.0027776	0.042105	0.065967	1067	0.94742	-0.079841	0.085396
{ 'RecDR' }	<b>0.29774</b>	<b>0.064784</b>	4.596	1067	<b>4.8222e-06</b>	0.17063	0.42486
{ 'RecThr:RecDR' }	<b>-0.0089509</b>	<b>0.0029048</b>	-3.0815	1067	<b>0.0021126</b>	-0.014651	-0.0032512



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

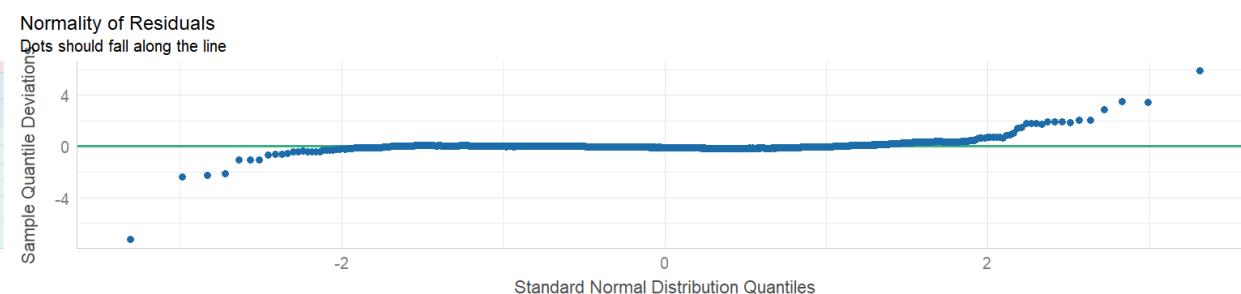
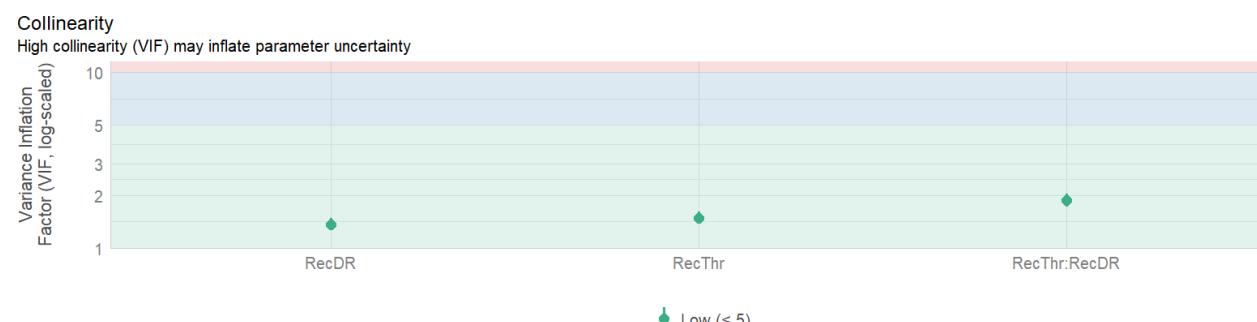
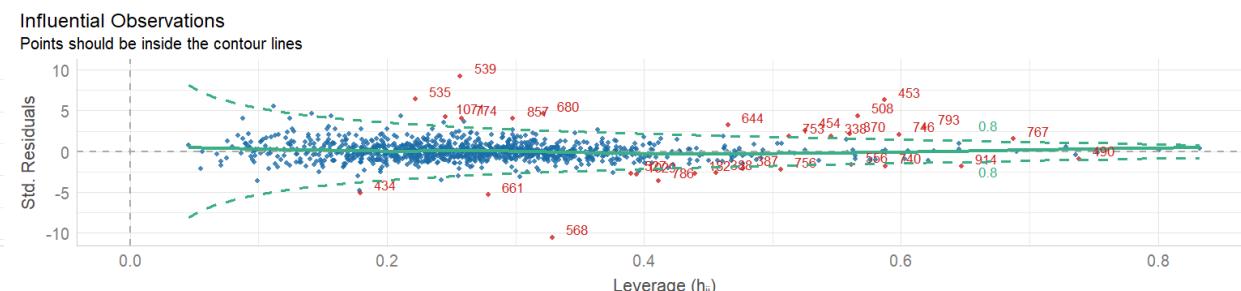
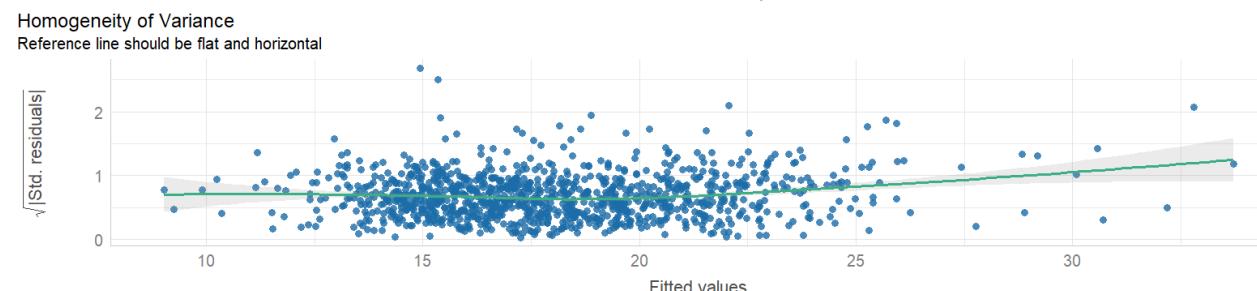
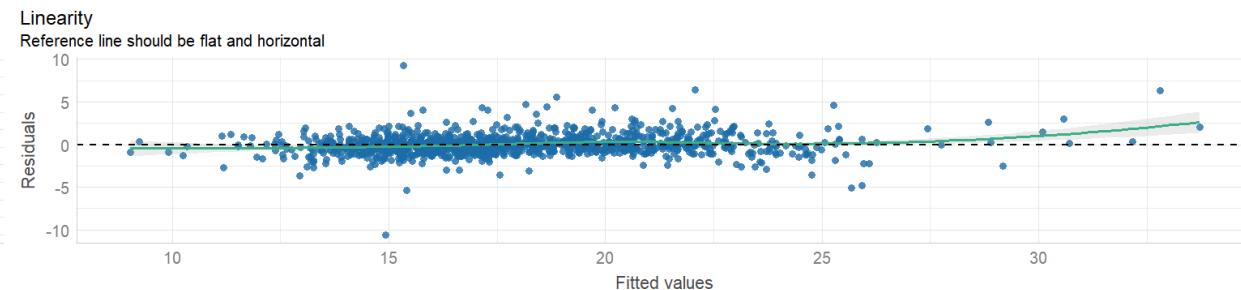
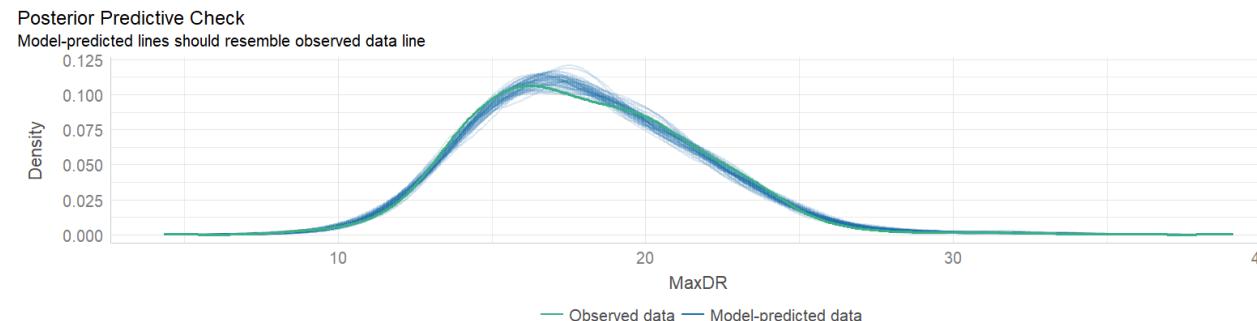
GA No. 10052152

Ground truth unknown!

# Experimental data: different LMEs in Rstudio



**MaxDR ~ 1 + RecThr\*RecDR + (1+RecThr|SubID) + (1+RecThr|SubID:ContRep)**  
 $+ (1+RecThr|SubID:MuId) + (1+RecDR|SubID:ContRep) + (1+RecDR|SubID:MuId)$



# Experimental data: different LMEs in Rstudio



```
MaxDR ~ 1 + RecThr*RecDR+(-1 + RecThr|ContRep) + (-1 + RecThr|SubID)+ ' ...  
' (-1 + RecThr|SubID:MUid) +(-1 + RecDR|ContRep) + (-1 + RecDR|SubID)+ (-1 + RecDR|SubID:MUid)
```

## MATLAB

Name	Estimate	SE	tStat	DF	pValue	Lower	Upper
{ '(Intercept)' }	<b>15.996</b>	<b>0.3341</b>	47.878	1067	<b>5.5495e-268</b>	15.34	16.652
{ 'RecThr' }	<b>0.0027776</b>	<b>0.042105</b>	0.065967	1067	0.94742	-0.079841	0.085396
{ 'RecDR' }	<b>0.29774</b>	<b>0.064784</b>	4.596	1067	<b>4.8222e-06</b>	0.17063	0.42486
{ 'RecThr:RecDR' }	<b>-0.0089509</b>	<b>0.0029048</b>	-3.0815	1067	<b>0.0021126</b>	-0.014651	-0.0032512

## Rstudio

	Estimate	Std. Error	df	t value	Pr(> t )
(Intercept)	<b>15.995797</b>	<b>0.334103</b>	918.950516	47.877	<b>&lt; 2e-16 ***</b>
RecThr	<b>0.002786</b>	<b>0.042110</b>	43.998670	0.066	0.94756
RecDR	<b>0.297771</b>	<b>0.064787</b>	44.772357	4.596	<b>3.51e-05 ***</b>
RecThr:RecDR	<b>-0.008952</b>	<b>0.002905</b>	953.703114	-3.082	<b>0.00212 **</b>
---					
Signif. codes:	0 '***'	0.001 '**'	0.01 '*'	0.05 '.'	0.1 ' '

Ground truth unknown!

# Experimental data: Bayesian linear regression



```
MaxDR ~ 1 + RecThr * RecDR + (-1 + RecThr | ContRep) + (-1 + RecThr | SubID) +  
(-1 + RecThr | SubID:MUid) + (-1 + RecDR | ContRep) + (-1 + RecDR | SubID) + (-1 + RecDR | SubID:MUid)
```

## Rstudio

Population-Level Effects:

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
Intercept	<b>16.02</b>	<b>0.36</b>	15.32	16.71	1.00	3181	3359
RecThr	<b>0.00</b>	<b>0.05</b>	-0.10	0.10	1.00	1306	1812
RecDR	<b>0.29</b>	<b>0.09</b>	0.11	0.46	1.00	984	1362
RecThr:RecDR	<b>-0.01</b>	<b>0.00</b>	-0.01	-0.00	1.00	3161	2940

Ground truth  
unknown!

Family Specific Parameters:

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
sigma	<b>1.48</b>	<b>0.04</b>	1.39	1.57	1.00	1852	2455

## MATLAB

Model not supported



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Summary of introduction to...



- Model assumptions important, but not always easy to reach
- Visual check of model assumptions requires experiences
- Different programming languages come with different support to linear regression models
  - Rstudio, MATLAB, Python, JASP...
- Numerous packages in Rstudio – time needed for their testing and selection
- Different schools of thinking:
  - Linear Mixed Effect
  - Bayesian Linear Regression
- Comparison of different data models
  - AIC & BIC for Linear Mixed Effect models
  - WAIC & LOO for Bayesian Linear Regression models
- Simulated data can serve as an easy-to-use platform for testing of different assumptions.



Funded by  
the European Union



UK Research  
and Innovation

GA No. 101079392

GA No. 10052152

# Literature



- Winter, B., 2013. **A very basic tutorial for performing linear mixed effects analyses.** *arXiv preprint arXiv:1308.5499*, pp.1-22.
- G. K. Hajduk, **Introduction to linear mixed models**, <https://ourcodingclub.github.io/tutorials/mixed-models>
- H. Schielzeth et al. **Robustness of linear mixed-effects models to violations of distributional assumptions**, <https://doi.org/10.1111/2041-210X.13434>
- S. A. Baldwin et al., **An introduction to using Bayesian linear regression with clinical data**, <https://doi.org/10.1016/j.brat.2016.12.016>
- M. Franke et al. **A tutorial on contrast coding for (Bayesian) regression**, <https://michael-franke.github.io/Bayesian-Regression/practice-sheets/01e-contrast-coding-tutorial.html>
- E. Makalic et al. **High-Dimensional Bayesian Regularised Regression with the BayesReg Package**, arXiv:1611.06649 [stat.CO] [Version 1.9.1.0](#) (105 KB) by [Statovic](#)
- **Stan** <https://mc-stan.org/> (different programming languages supported, R, Matlab...)



Funded by  
the European Union

GA No. 101079392



UK Research  
and Innovation

GA No. 10052152

February 6<sup>th</sup> –9<sup>th</sup> 2024

Universitat Politècnica de Catalunya, Barcelona, Spain



HYBRID  
NEURO

# WORKSHOP BCN24

## “A journey into brain activity”

*From EEG and related potentials to connectivity and source modeling*

**Day 1: EEG signal acquisition and preprocessing.**

**Day 2: ERP and MRCP studies and movement intention for device control.**

**Day 3: Source localization and brain connectivity.**

**Day 4: Networking with hospitals, companies, and research centers.**



Hybrid Workshop  
(online and In-person event).  
Contact: Bioart.group@upc.edu



REGISTER NOW



Funded by  
the European Union



UK Research  
and Innovation

GA 10052152



University of Maribor



UNIVERSITAT POLITÈCNICA  
DE CATALUNYA  
BARCELONATECH



CHALMERS  
UNIVERSITY OF TECHNOLOGY

Imperial College  
London

GA 101079392

February 6<sup>th</sup> –9<sup>th</sup> 2024

Universitat Politècnica de Catalunya, Barcelona, Spain



HYBRID  
NEURO

DAY	Tuesday 6th	Wednesday 7th	Thursday 8th	Friday 9th
	EEG signal acquisition and preprocessing	ERP and MRCP studies and movement intention for device control	Source localization and brain connectivity	Networking with hospitals, companies, and research centers
Presentations	09:30-10:00	Related cortical potentials measured by EEG: ERPs and MCRPs	EEG source imaging: a practical review	What HybridNeuro Hub can do for you and you for it
	10:00-10:30	Presentation of HybridNeuro Action and UPC		Hospitals and companies presentations (I part)
	10:30-11:00	Computerized computing tasks: cognitive and motor exercises		
	11:00-11:30	COFFEE BREAK	COFFEE BREAK	COFFEE BREAK
	11:30-12:30	Types of EEG artifacts and how to handle with them	ML and DL methods for movement imaginary BCI: Challenges and future directions	Introduction to functional Brain connectivity
	12:30-13:30	Artifact rejection and reduction by signal processing	Neuro-interfaces for interacting with robotics exoskeletons	Brain networks analysis using graph theory parameters
	13:30-15:00	LUNCH	LUNCH	LUNCH
	15:00-17:00	Artifact reduction using software packages	A MRCP study: experiment preparation, recording and analysis	Practicing brain source localization and functional connectivity
HoT				



Funded by  
the European Union



UK Research  
and Innovation

GA 10052152



University of Maribor



UNIVERSITAT POLITÈCNICA  
DE CATALUNYA  
BARCELONATECH



CHALMERS  
UNIVERSITY OF TECHNOLOGY

Imperial College  
London



University of Maribor



Imperial College  
London



REGISTER NOW!



UK Research  
and Innovation

GA No. 10052152



Funded by  
the European Union

GA No. 101079392



**FREE REGISTRATION**  
Travel & accommodation costs  
to be covered by participants



# Summer school on **Hybrid Neural Interfaces**

**July 8<sup>th</sup>-12<sup>th</sup> 2024, Maribor, Slovenia**

- Surface & intramuscular HDEMG
- Identification of neural codes
- EEG & functional brain connectivity
- Corticomuscular coupling
- Movement augmentation
- Hybrid Neural Interfaces in practice
- Keynote lectures
- Practical examples
- Student 2 student explanations
- Present your project
- Ask top experts
- Active consultations



# Questions?



**Funded by  
the European Union**



**UK Research  
and Innovation**

This project has received funding from the European Union's Horizon Europe Research and Innovation Programme under grant agreement no. 101079392 and from the UK Research and Innovation (UKRI) government's Horizon Europe funding guarantee scheme under grant agreement no. 10052152.